

CAHD

Computer-aided hopper design

A short introduction

Motivation

Present situation

The original application of shear testers is silo design for flow based on Jenike's fundamental contribution around 1960 (e.g., Bulletin 123).

Jenike's original equations can only be solved numerically (great effort for day-to-day business, especially at that time). Thus, Jenike provided design charts for hopper design.

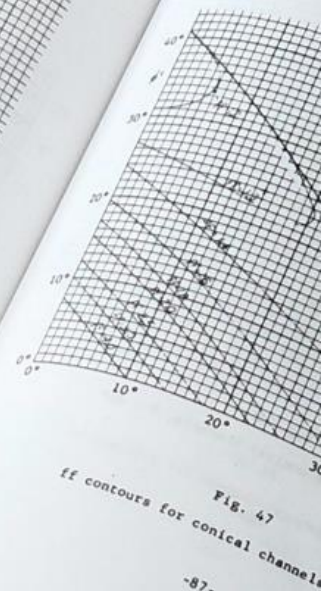
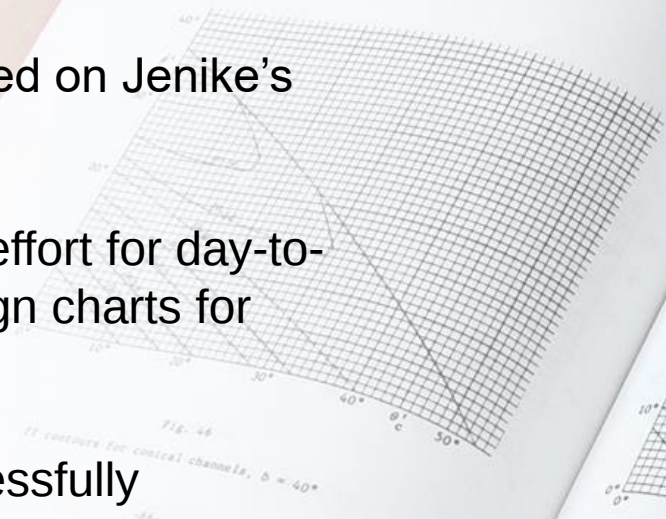
→ Big step forward, thousands of silos have been designed successfully

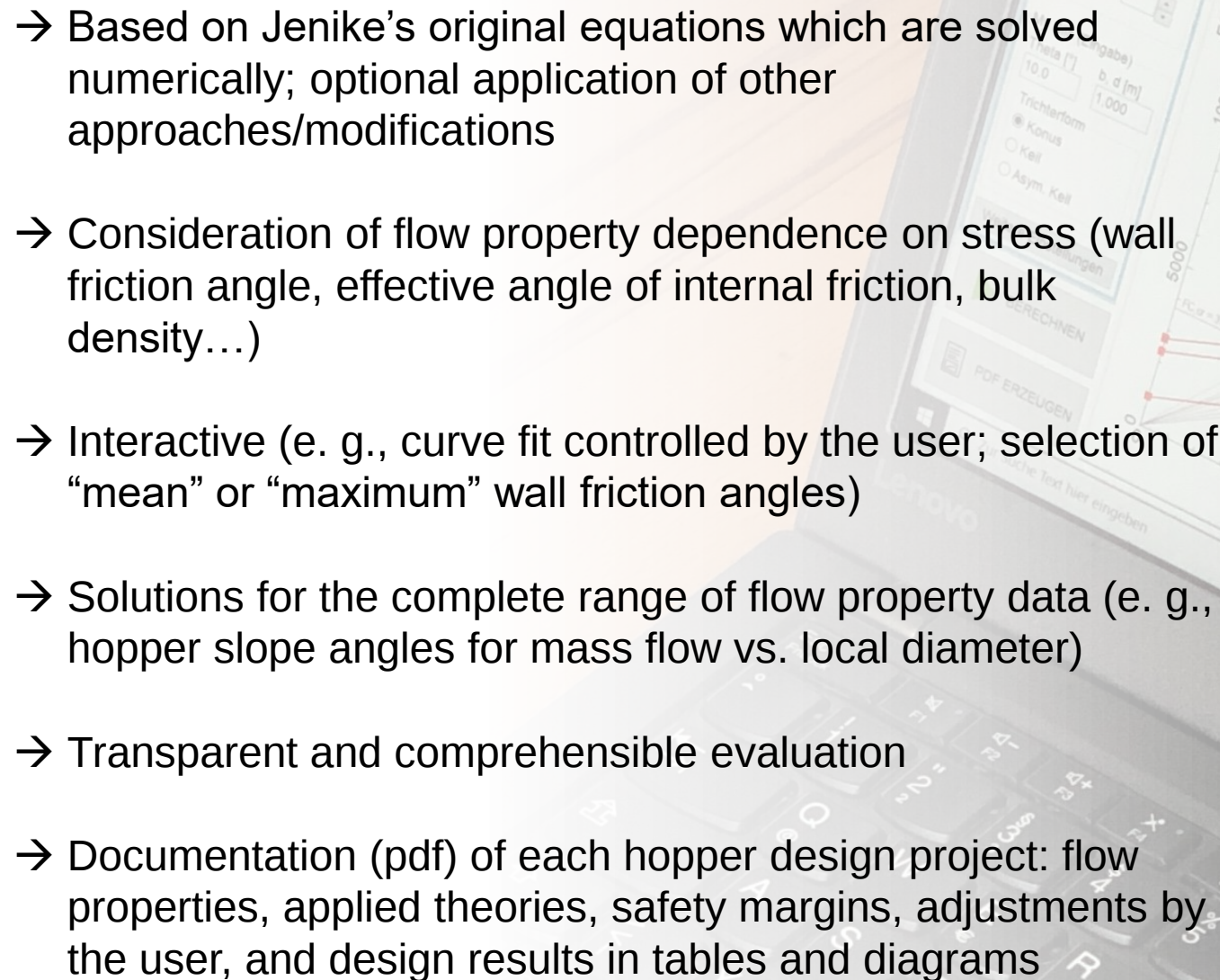
The application of design charts can be time-consuming (often iteration is required; variation of hopper geometry or parameters such as wall friction increases the effort). Therefore, there is a demand for software solutions.

These exist, mostly based on approximate equations such as those derived by Arnold and McLean:

→ Self-made EXCEL[®] tools (Documentation? Transfer to job successors?)

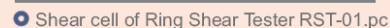
→ Simple "hopper design" functions in shear test evaluation software



- 
- Based on Jenike's original equations which are solved numerically; optional application of other approaches/modifications
 - Consideration of flow property dependence on stress (wall friction angle, effective angle of internal friction, bulk density...)
 - Interactive (e. g., curve fit controlled by the user; selection of "mean" or "maximum" wall friction angles)
 - Solutions for the complete range of flow property data (e. g., hopper slope angles for mass flow vs. local diameter)
 - Transparent and comprehensible evaluation
 - Documentation (pdf) of each hopper design project: flow properties, applied theories, safety margins, adjustments by the user, and design results in tables and diagrams

The program

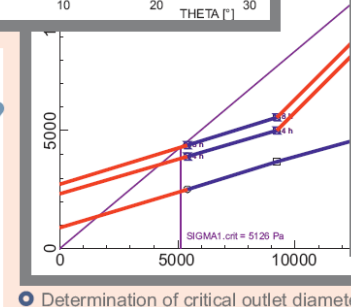
1 Measure the bulk solid's flow properties (Ring Shear Tester and control software RST-CONTROL 95)



2 Test results: Strength, bulk density, internal friction, wall friction, and time consolidation

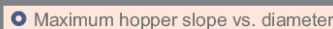


20000



Page of final report (slope vs. diameter)

3 Computer-aided hopper design: Program generates ff-diagrams, interactively determines outlet dimensions and hopper angles, and creates a final report.



- Determination of critical outlet diameter

Data import (Schulze ring shear testers, Jenike shear tester)



Ring Shear Tester RST-01.01

Software: RSV 95

→ EIF files (EIF: extended input file)

Ring Shear Tester RST-01.pc

Software: RST-CONTROL 95

→ EIF files (EIF: extended input file)

→ FPE files (FPE: flow properties exchange file)



Ring Shear Tester RST-XS

Software: RST-CONTROL 95

→ EIF files (EIF: extended input file)

→ FPE files (FPE: flow properties exchange file)

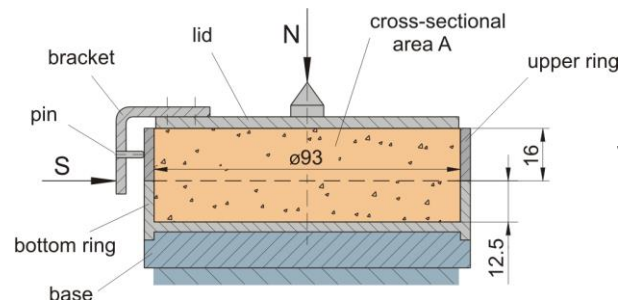


Ring Shear Tester RST-XS

Software: RST-CONTROL 95

→ EIF files (EIF: extended input file)

→ FPE files (FPE: flow properties exchange file)



Jenike-type Shear Tester

Software: SV 95

→ FPE files (FPE: flow properties exchange file)

Import of flow properties from other sources

Template for Microsoft EXCEL[®]
→ CSV file

Caution! Data must have been obtained with **reliable** testers.

	A	B	C	D	E	F	G	H	I	J	K	L
1	Input File for CAHD				Version 10000							
2												
3	Bulk Solid:	X powder										
4	Order:	No. 1										
5												
6	Units:	Stress		Density		Time						
7		Pa		kg/m3		h						
8												
9	Flow properties (instantaneous)											
10	YL No.	SIGMA1	FC	RHOB	PHIE	PHILIN						
11	1	5417	2524	1059	51,2	38,6						
12	2	9238	3672	1103	47,8	37,1						
13	3	18314	6207	1177	45,7	36,8						
14	4											
15	5											
16	6											
17	7											
18	8											
19	9											
20	10											
21												
22	Time consolidation											
23		Time t:	4	8								
24	Accord. to YL:	SIGMA1	FC(t1)	FC(t2)	FC(t3)	FC(t4)	FC(t5)	FC(t6)	FC(t7)	FC(t8)	FC(t9)	FC(t10)
25	1	5417	3909									
26	2	9238	6054	8400								
27	3	18314	7777	10239								
28	4	0										
29	5	0										
30	6	0										
31	7	0										
32	8	0										
33	9	0										
34	10	0										
35												
36	Wall friction #1											
37	Wall material:	Mild steel										
38	Stress level	SIGMAW	PHIX,MIN	PHIX,M	PHIX,MAX							
39	1	701	30,1	30,9	31,8							
40	2	2150	29,2	29,7	30,1							
41	3	3599	29,2	29,4	29,4							
42	4	5048	28,6	29	29,6							
43	5	6497	28,4	28,8	29,1							
44	6	7946	27,9	28,7	29,1							
45	7											
46	8											
47	9											
48	10											
49												
50	Wall friction #2											
51	Wall material:											
52	Stress level											
53	1											
54	2											
55	3											

Create CSV

Sprache/Language:

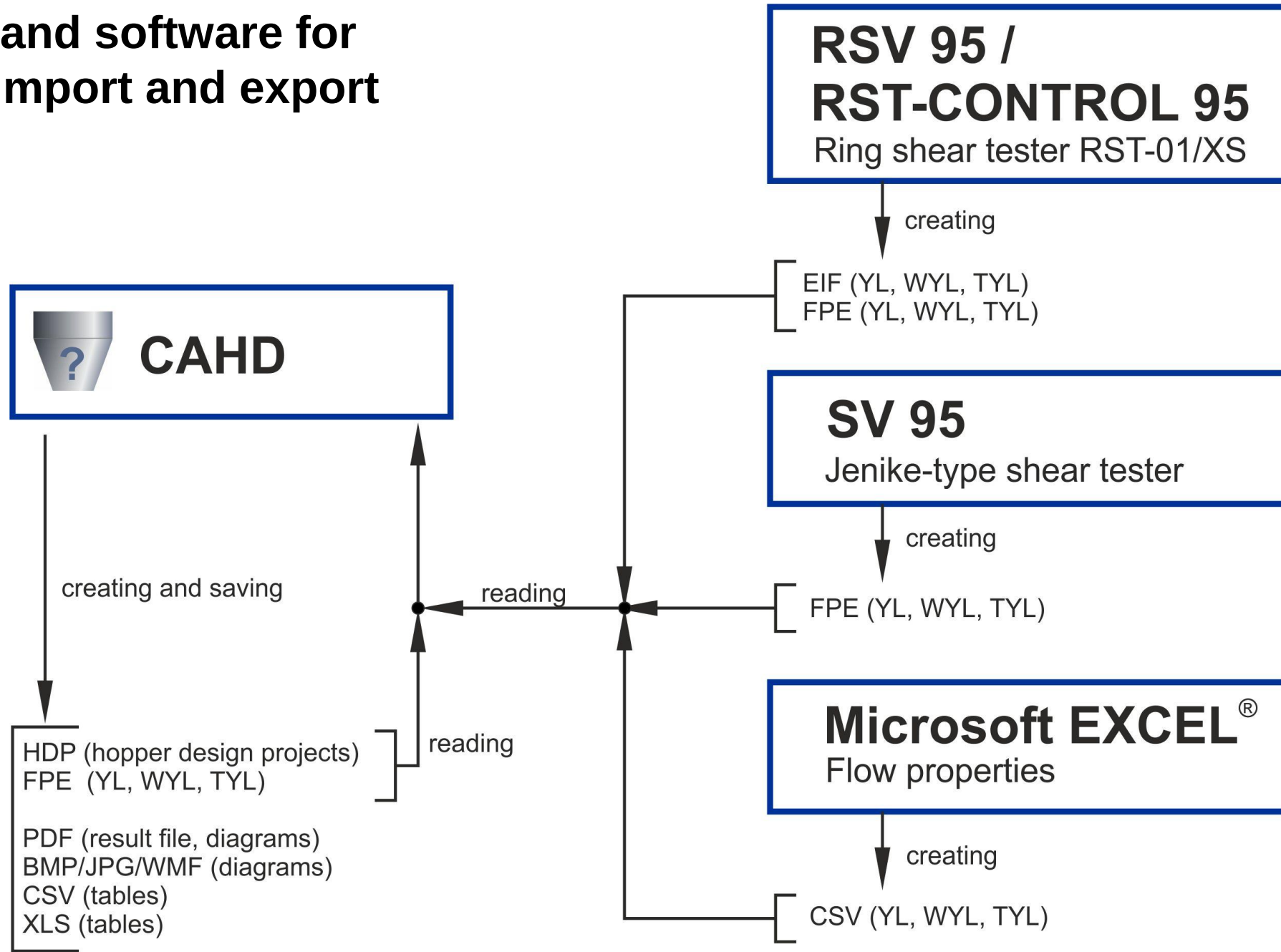
Deutsch English

Clear form:

Delete all entries

RHOB,f

Files and software for data import and export



Applied theories and options

A. W. Jenike (Bull. 123) 1964/1980

- Mass flow: Arching
- Funnel flow: Ratholing (lower/upper bound), Arching

ff-values and mass flow boundaries have been calculated for φ_e varied in steps of 1°

Option: extended range $\varphi_e = 20^\circ$ to $\varphi_e = 80^\circ$.

Option

O. Molerus:

Smaller ff-values for steep hoppers / low wall friction

Option

P. C. Arnold / A. G. McLean:

Analytical flow factors ff (based on G. Enstad's approach)

Option

A. W. Roberts:

Ratholing: Modification of Jenike's upper bound approach (considering anisotropic behaviour)

Working with the program



CAHD v1.0

Yield loci (diagram)

☐ 1

☐ 2

☐ 3

☐ 4

☐ 5

☐ 6

☐ 7

☐ 8

☐ 9

☐ 10

All

No

Diagram type

Yield locus/loci

Options

Full screen

☒ Legend

☒ SIGMA1 Mohr circle

☒ FC Mohr circle

☐ PHIE line

☒ Data points

☒ Lines

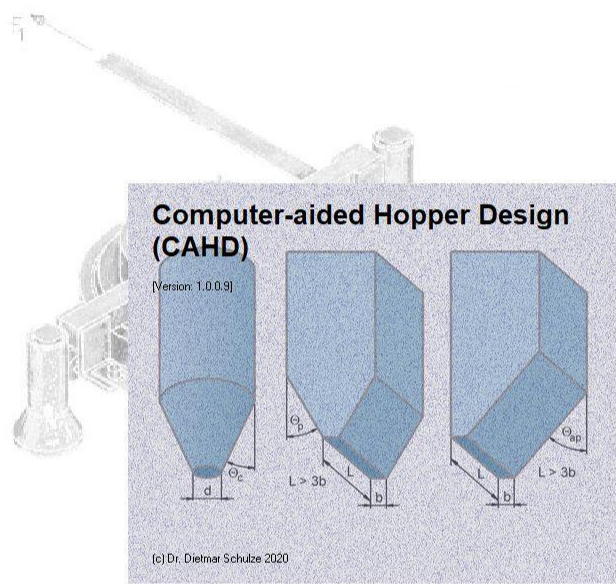
☐ Regr.

☐ Grid

☐ FFC = 1; 2; 4; 10

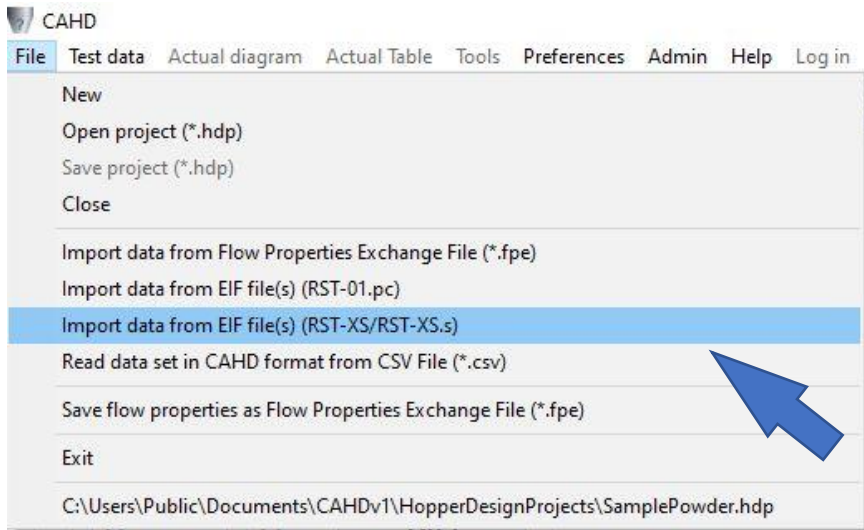
☐ FFC = 1; 1.2 .. 2.0

☐ FFC = 0



CAHD splash screen

No.	SIGMA1 [kPa]	FC [kPa]	FFC	FFRHO	TAU,C [kPa]	RHOB [kg/m3]	PHIE [°]	PHILIN [°]	PHISF [°]	Bulk Solid	Order
1											
2											
3											
4											
5											
6											

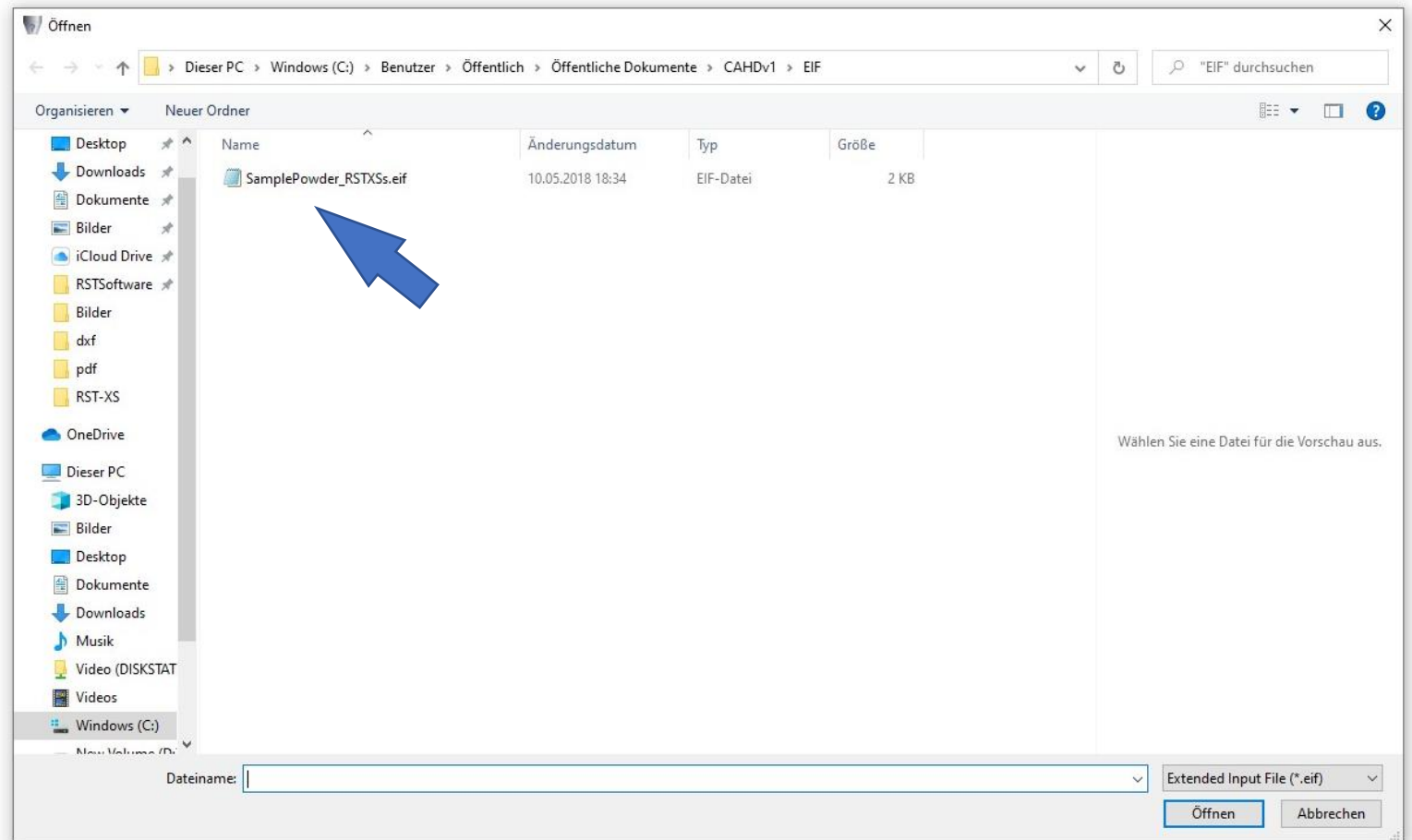


Hopper Design

Import of flow properties from EIF file
(here: measured with Ring Shear Tester RST-XS.s)

Diagram type

Yield locus/loci



Yield loci (diagram)

☐ 1☐ 5☐ 9

☐ 2☐ 6☐ 10

☐ 3☐ 7

All

☐ 4☐ 8

No

Diagram type

Yield locus/loci

Options

Full screen

☒ Legend

☒ SIGMA1 Mohr circle

☒ FC Mohr circle

☐ PHIE line

☒ Data points

☒ Lines☐ Reqr.

☐ ☐ Grid

☐ FFC = 1; 2; 4; 10

☐ FFC = 1; 1.2 .. 2.0

☐ FFC =

CAHD shows contents of EIF file.
Flow properties to be imported are selected.

Choice of data to append

Yield loci:

☒ Sample Powder ; XYZ Ltd. ; N,pre = 1.05697 kg

☒ Sample Powder ; XYZ Ltd. ; N,pre = 1.90234 kg

☒ Sample Powder ; XYZ Ltd. ; N,pre = 3.80467 kg

Time yield loci corresponding to yield locus::

☒ Time yield loci corresp. to yield locus no. 1

☒ Time yield loci corresp. to yield locus no. 2

Wall yield loci:

☒ Sample Powder ; XYZ Ltd. ; Mild steel St37

Uncheck all

Check all

CANCEL

OK



No.	SIGMA1 [kPa]	FC [kPa]	FFC	FFRHO	TAU,C [kPa]	RHOB [kg/m3]	PHIE [°]	PHILIN [°]	PHISF [°]	Bulk Solid	Order
1											
2											
3											
4											
5											
6											

Yield loci (diagram)

☒ 1 ☐ 5 ☐ 9

☒ 2 ☐ 6 ☐ 10

☒ 3 ☐ 7

☐ 4 ☐ 8

Diagram type

Options

☒ Legend

☒ SIGMA1 Mohr circle

☒ FC Mohr circle

☐ PHIE line

☒ Data points

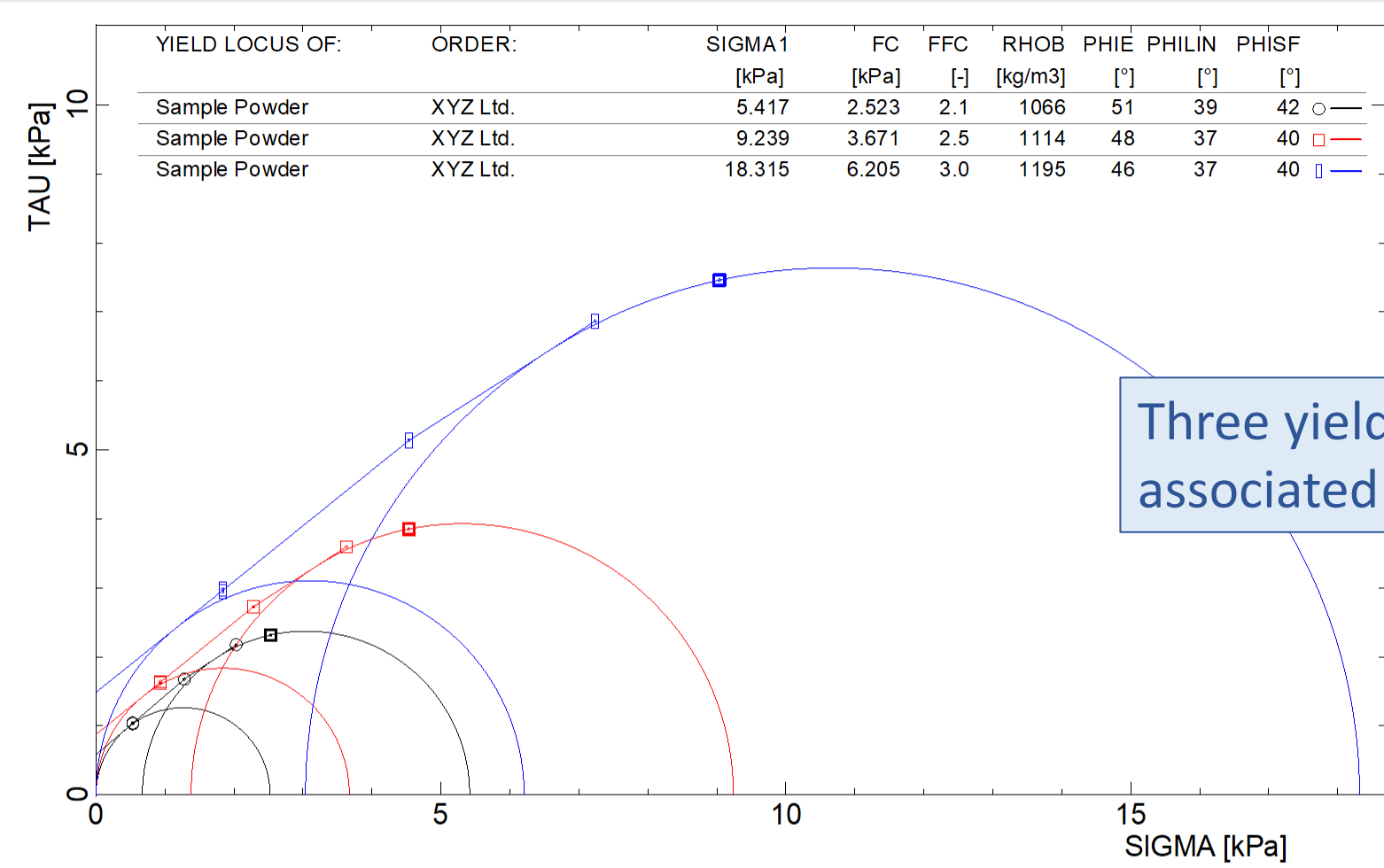
☒ Lines ☐ Regr.

☐ Grid

☐ FFC = 1; 2; 4; 10

☐ FFC = 1; 1.2 .. 2.0

☐ FFC =



Three yield loci and associated flow properties

No.	SIGMA1 [kPa]	FC [kPa]	FFC	FFRHO	TAU,C [kPa]	RHOB [kg/m3]	PHIE [°]	PHILIN [°]	PHISF [°]	Bulk Solid	Order
1	5.417	2.523	2.15	2.29	0.581	1066	51.2	38.6	42.5	Sample Powder	XYZ Ltd.
2	9.239	3.671	2.52	2.80	0.874	1114	47.8	37.1	40.4	Sample Powder	XYZ Ltd.
3	18.315	6.205	2.95	3.53	1.485	1195	45.7	36.8	39.5	Sample Powder	XYZ Ltd.
4											
5											
6											

Wall yield locus no.

☒ 1 ☐ 5 ☐ 9

☐ 2 ☐ 6 ☐ 10

☐ 3 ☐ 7

☐ 4 ☐ 8

Diagram type

☒ Wall yield locus

☐ PHIX = f(SIGMA,w)

Options

☒ Legend

☒ Data points

☒ Lines

☐ Grid

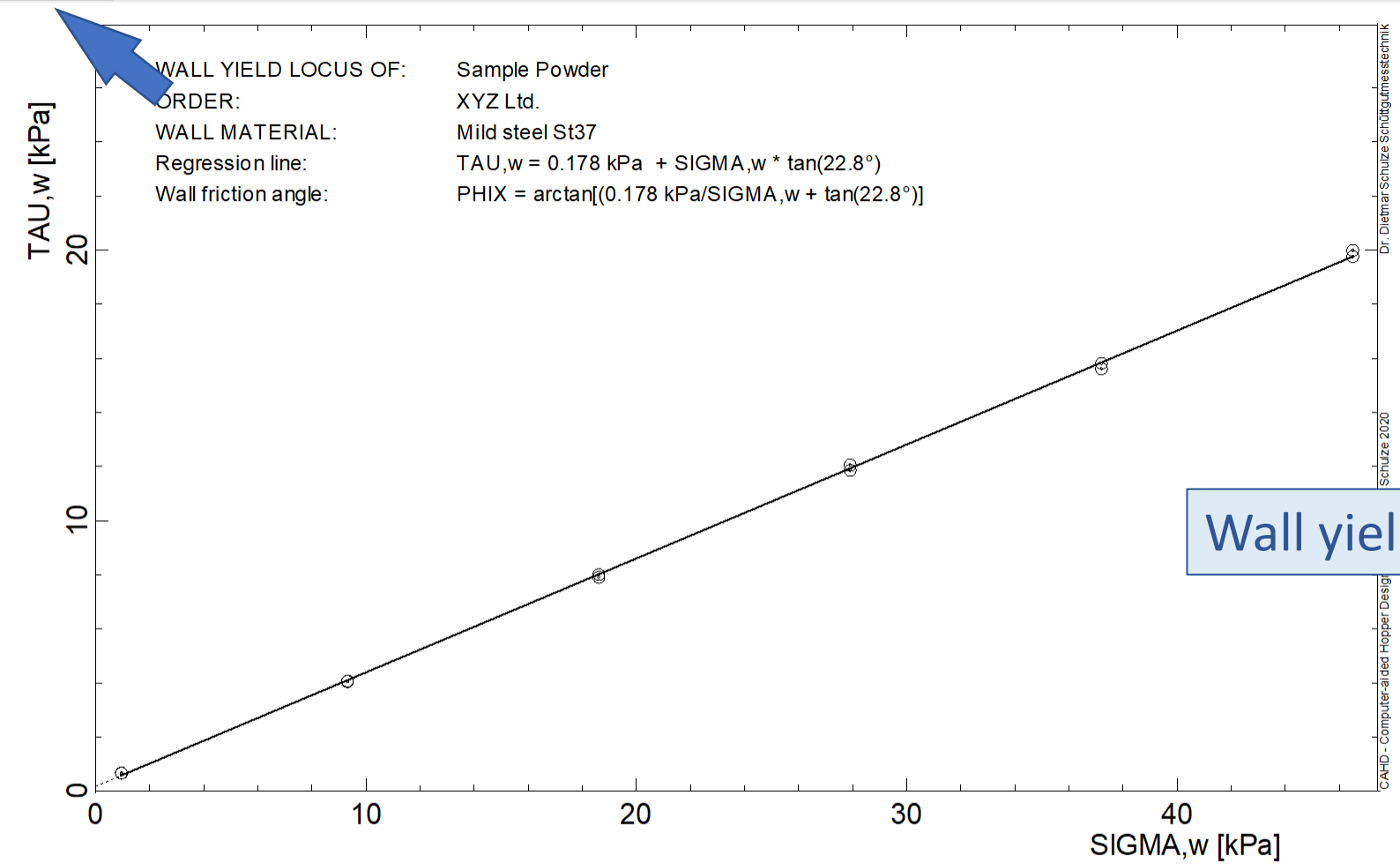
☐ Min. values

☐ Max. values

☐ Range x-axis

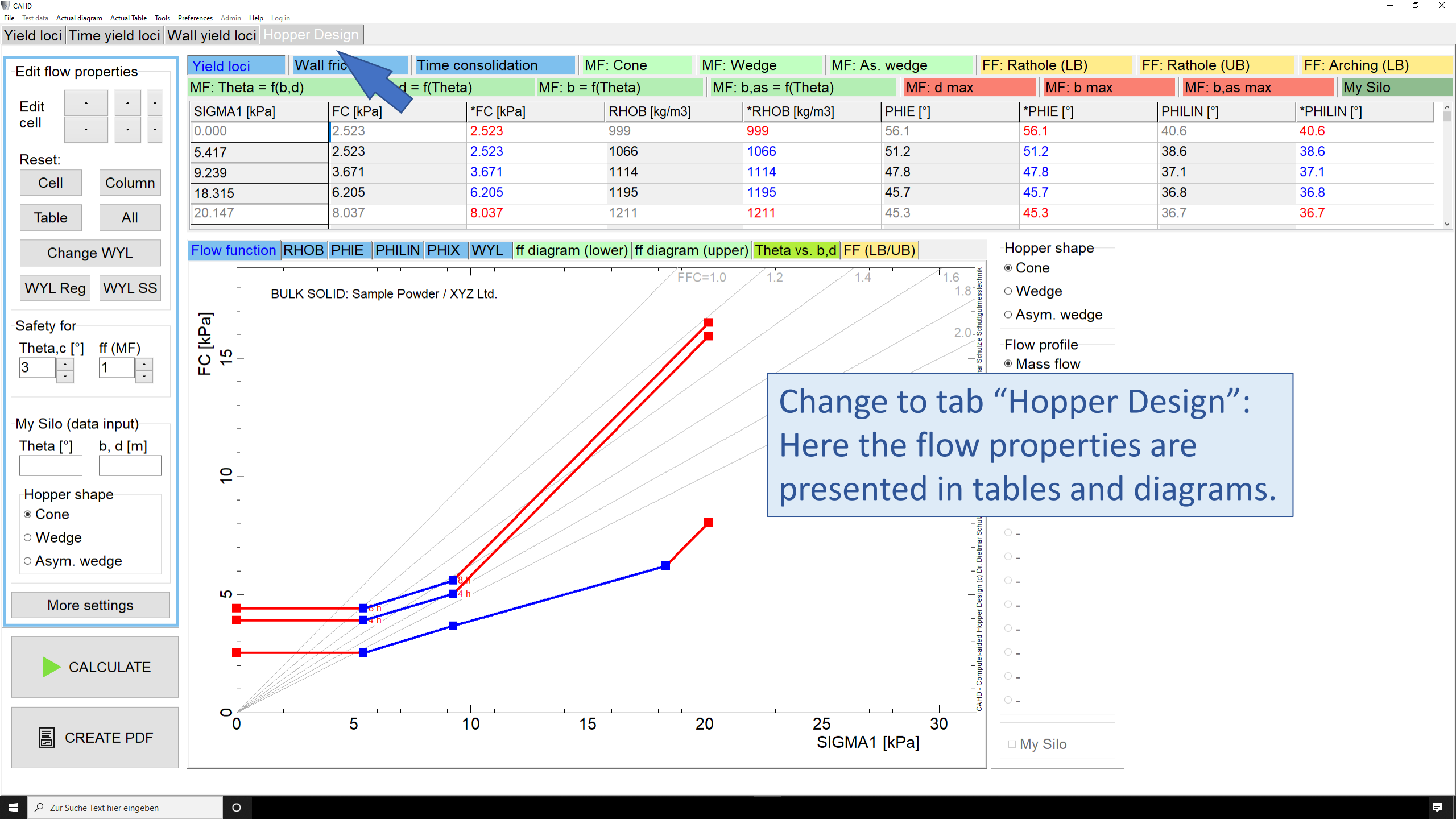
[kPa]

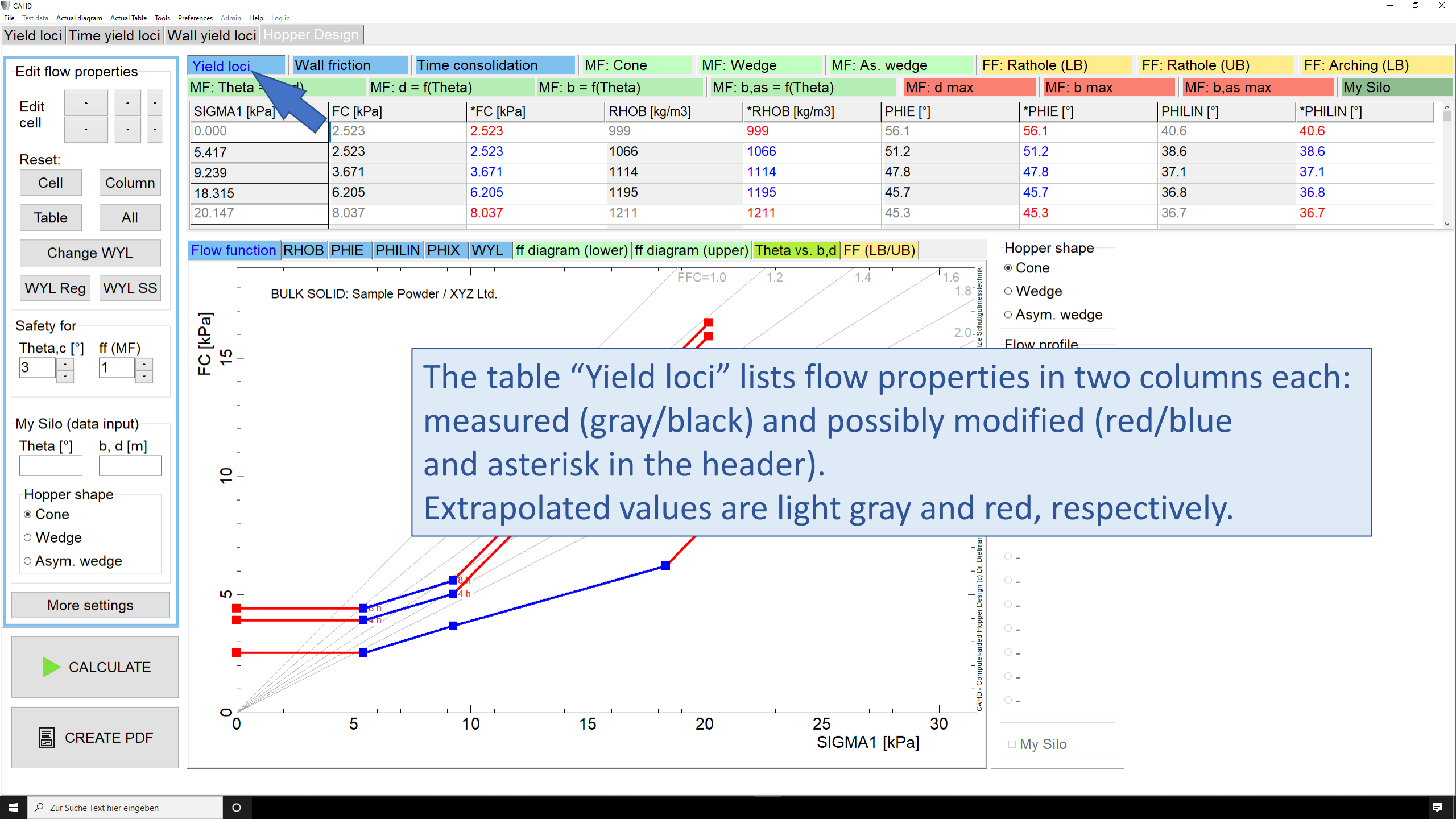
☐ Black and white



Wall yield locus no. 1:

SIGMA,w [kPa]	PHIX,min [°]	PHIX,m [°]	PHIX,max [°]	SIGMA,w [kPa]	PHIX,min [°]	PHIX,m [°]	PHIX,max [°]
0.955	34.7	34.9	35.1				
9.320	23.5	23.6	23.6				
18.613	23.0	23.1	23.3				
27.907	23.0	23.2	23.4				
37.200	22.8	22.9	23.0				
46.494	23.0	23.2	23.3				





Edit flow properties

Edit cell

Reset:

Cell Column

Table All

Change WYL

WYL Reg WYL SS

Safety for

Theta, c [°]	ff (MF)
3	1

My Silo (data input)

Theta [°]	b, d [m]

Hopper shape

- ☒ Cone
- ☐ Wedge
- ☐ Asym. wedge

More settings

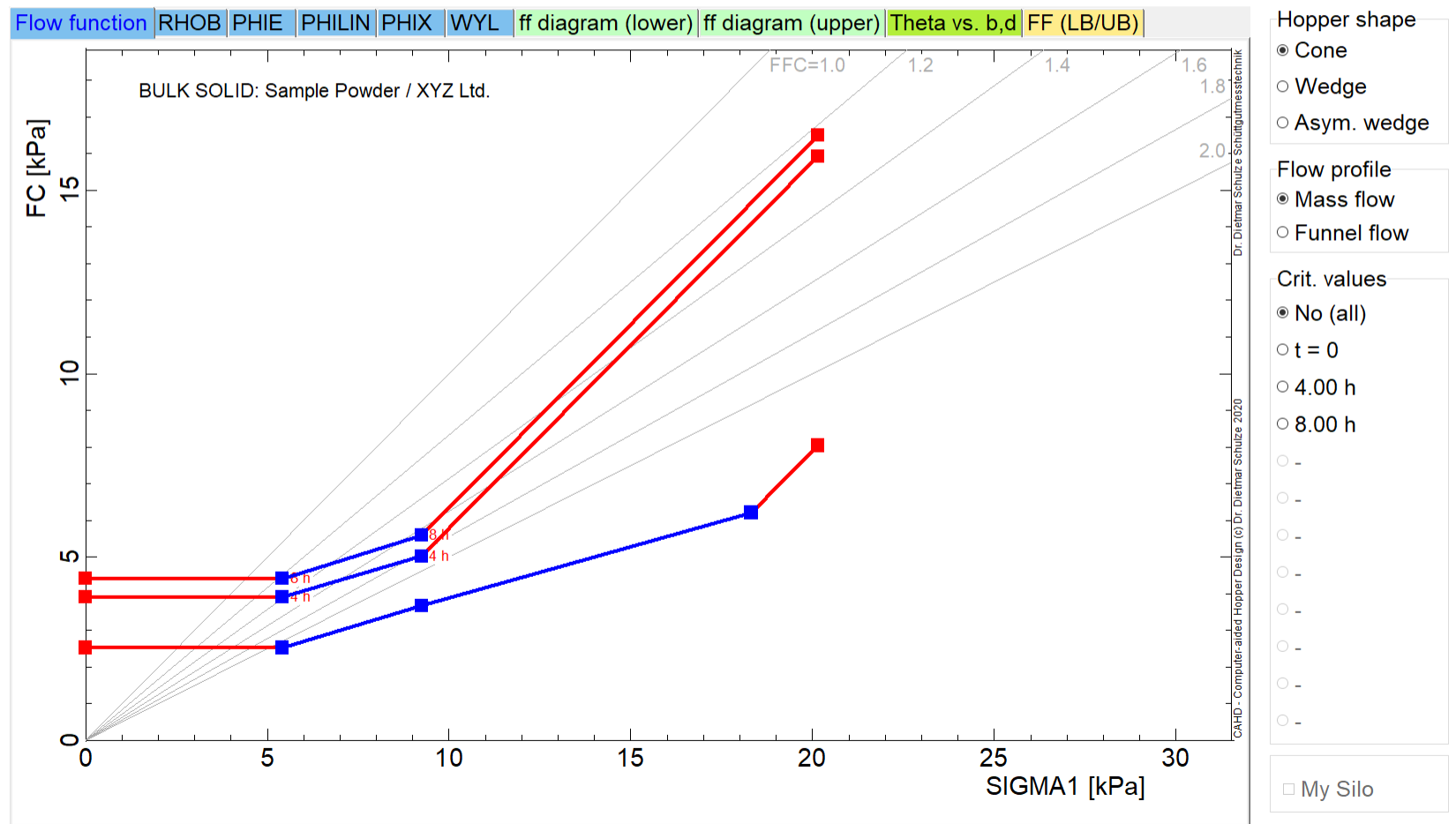
 CALCULATE

 CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
SIGMA1 [kPa] t [h]	4.00	*4.00	8.00	*8.00				
0.000	3.907	3.907	4.404	4.404				
5.417	3.907	3.907	4.404	4.404				
9.239	5.025	5.025	5.587	5.587				
18.315								
20.147	15.932	15.932	16.495	16.495				

Table with results of time consolidation tests.

Table with results of time consolidation tests.



Edit flow properties

Edit cell

↑

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↕

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

Hopper shape

☒ Cone

☐ Wedge

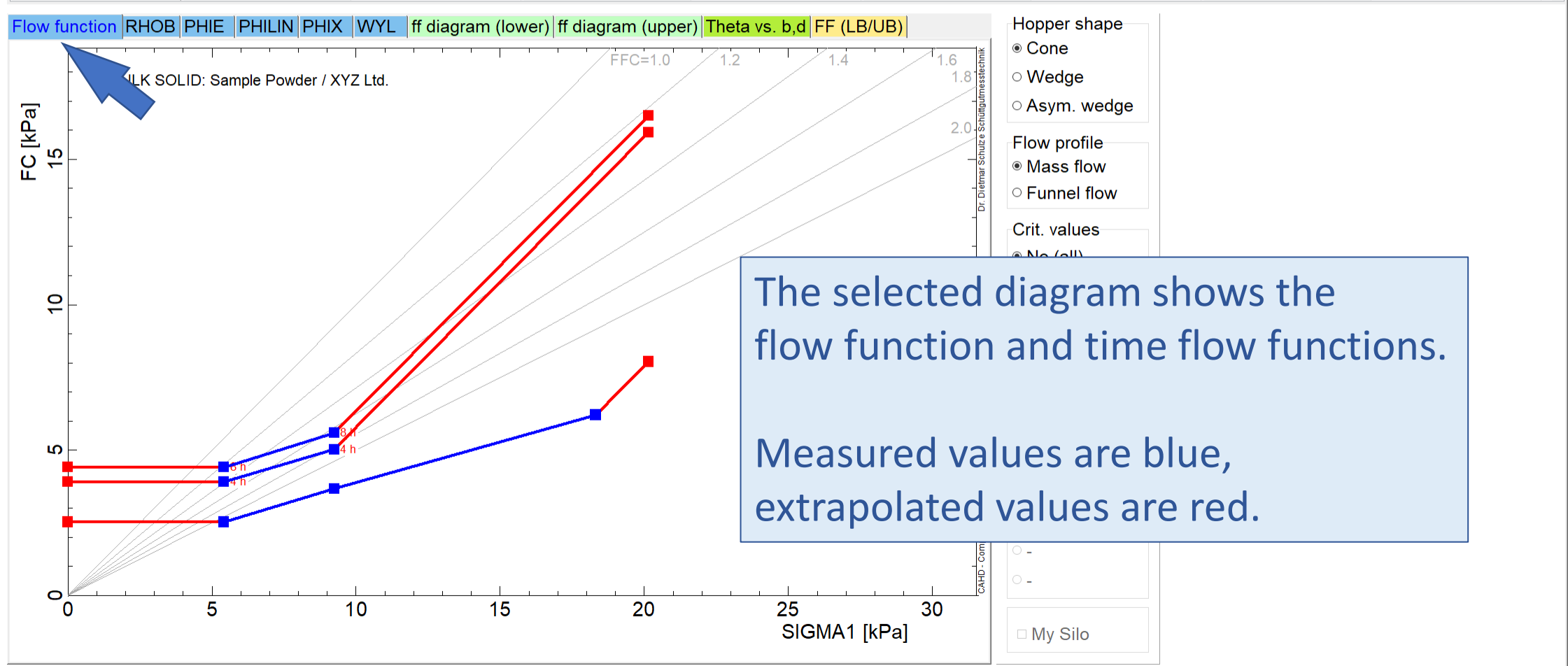
☐ Asym. wedge

More settings

CALCULATE

CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
SIGMA1 [kPa]	FC [kPa]	*FC [kPa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]
0.000	2.523	2.523	999	999	56.1	56.1	40.6	40.6
5.417	2.523	2.523	1066	1066	51.2	51.2	38.6	38.6
9.239	3.671	3.671	1114	1114	47.8	47.8	37.1	37.1
18.315	6.205	6.205	1195	1195	45.7	45.7	36.8	36.8
20.147	8.037	8.037	1211	1211	45.3	45.3	36.7	36.7



Edit flow properties

Edit cell

▲

▼

▲

▼

▲

▼

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta, c [°]

ff (MF)

3

▲

▼

1

▲

▼

My Silo (data input)

Theta [°]

b, d [m]

Hopper shape

☒ Cone

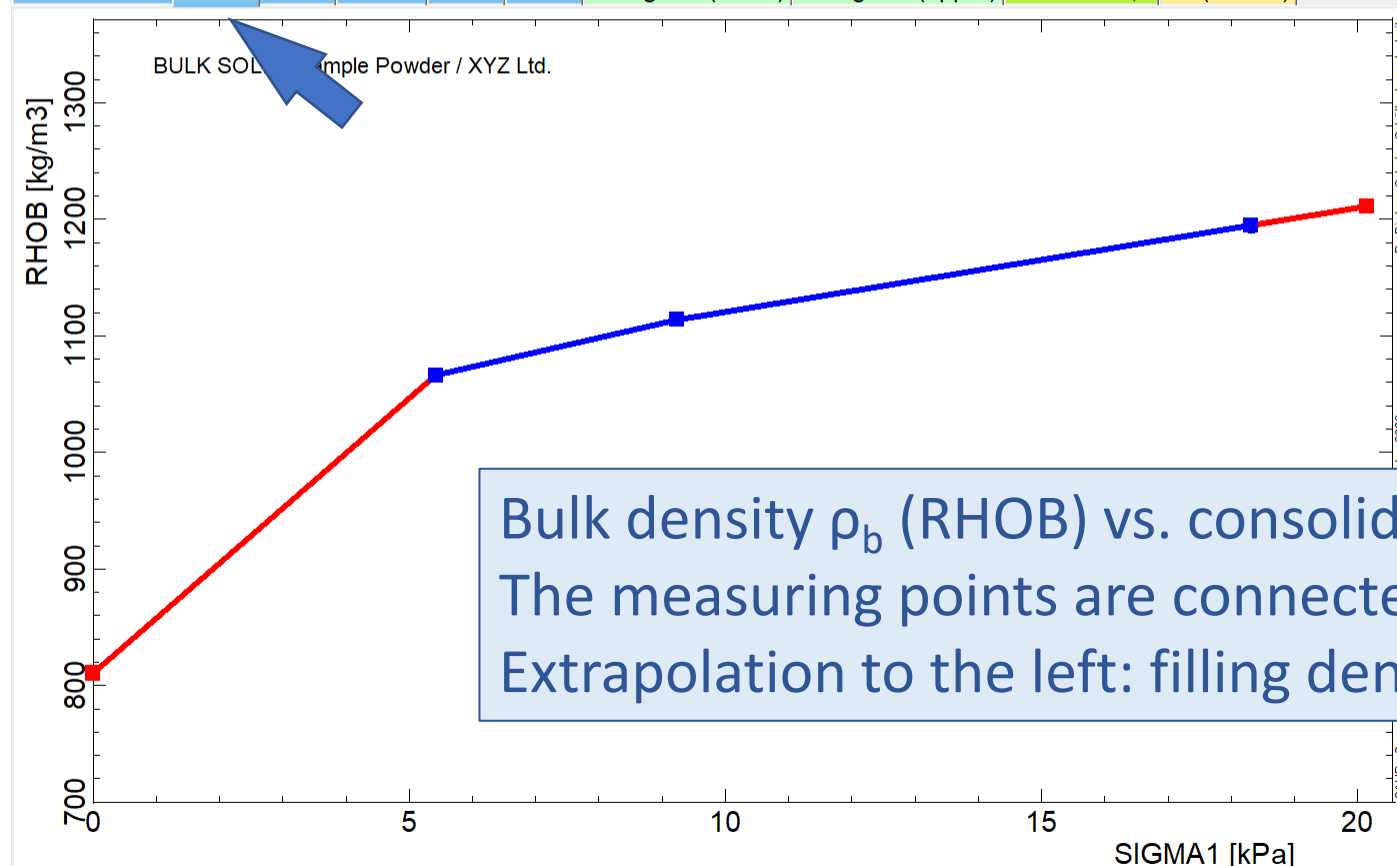
☐ Wedge

☐ Asym. wedge

More settings

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)	
MF: Theta = f(b,d)		MF: d = f(Theta)		MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo
SIGMA1 [kPa]	FC [kPa]	*FC [kPa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]	
0.000	2.523	2.523	811	811	56.1	56.1	40.6	40.6	
5.417	2.523	2.523	1066	1066	51.2	51.2	38.6	38.6	
9.239	3.671	3.671	1114	1114	47.8	47.8	37.1	37.1	
18.315	6.205	6.205	1195	1195	45.7	45.7	36.8	36.8	
20.147	8.037	8.037	1211	1211	45.3	45.3	36.7	36.7	

Flow function	RHOB	PHIE	PHILIN	PHIX	WYL	ff diagram (lower)	ff diagram (upper)	Theta vs. b,d	FF (LB/UB)
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Hopper shape

- ☒ Cone
- ☐ Wedge
- ☐ Asym. wedge

Flow profile

- ☒ Mass flow
- ☐ Funnel flow

Crit. values

- ☒ No (all)
- ☐ $t = 0$
- ☐ 4.00 h
- ☐ 8.00 h

Bulk density ρ_b (RHOB) vs. consolidation stress σ_1 (SIGMA1)
The measuring points are connected with lines.
Extrapolation to the left: filling density, $\rho_{b,f}$ (optional)

☐ -

☐ -

☐ My Silo

Edit flow properties

Edit cell

↑

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↑

↓

↑

↓

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

Hopper shape

☒ Cone

☐ Wedge

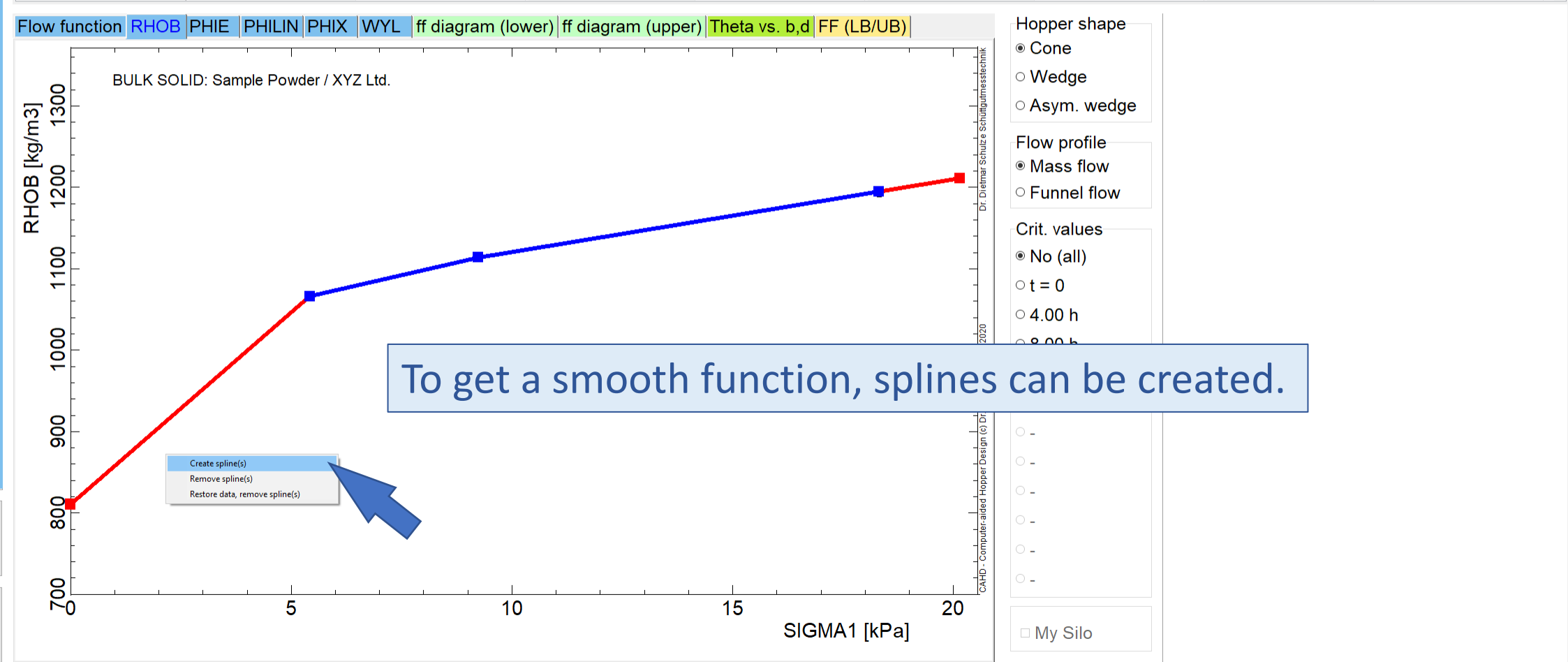
☐ Asym. wedge

More settings

CALCULATE

CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
SIGMA1 [kPa]	FC [kPa]	*FC [kPa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]
0.000	2.523	2.523	811	811	56.1	56.1	40.6	40.6
5.417	2.523	2.523	1066	1066	51.2	51.2	38.6	38.6
9.239	3.671	3.671	1114	1114	47.8	47.8	37.1	37.1
18.315	6.205	6.205	1195	1195	45.7	45.7	36.8	36.8
20.147	8.037	8.037	1211	1211	45.3	45.3	36.7	36.7



Edit flow properties

Edit cell

▲

▼

▲

▼

▲

▼

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

Hopper shape

☒ Cone

☐ Wedge

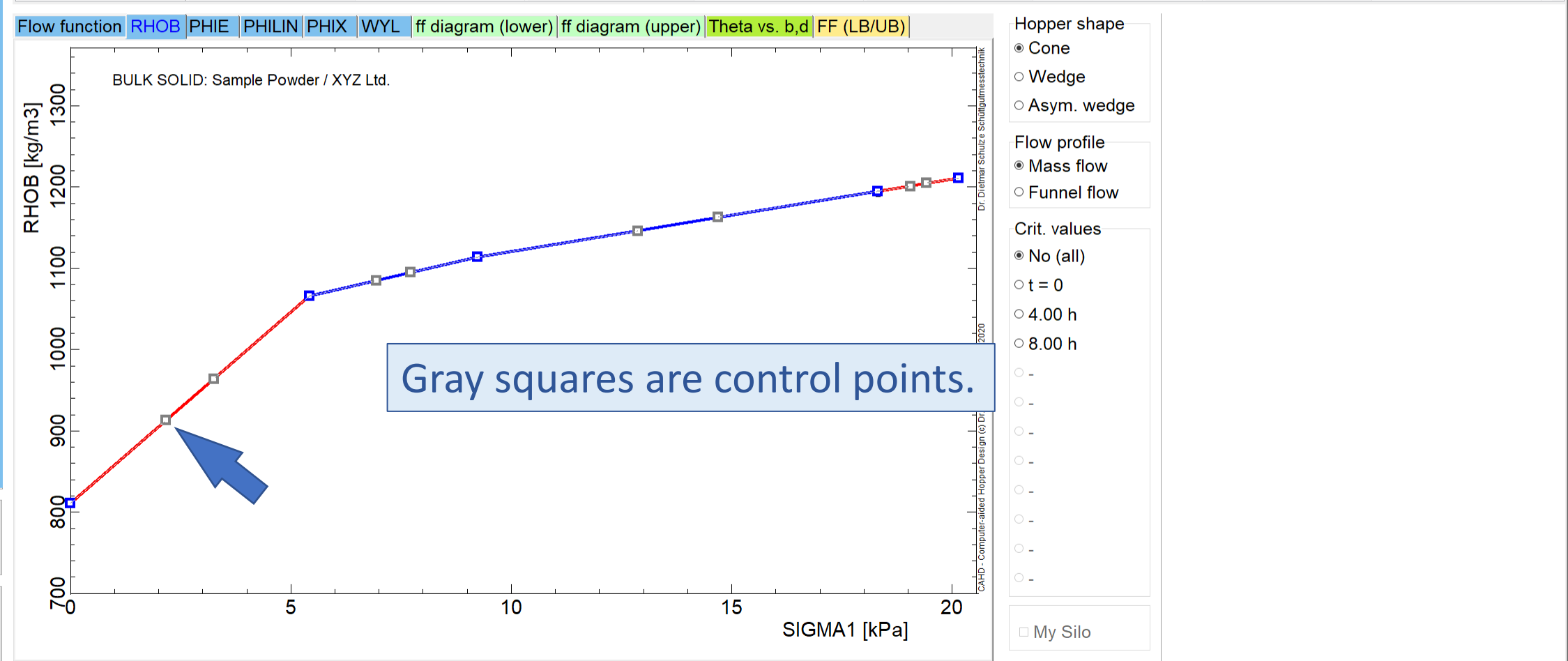
☐ Asym. wedge

More settings

CALCULATE

CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
SIGMA1 [kPa]	FC [kPa]	*FC [kPa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]
0.000	2.523	2.523	811	811	56.1	56.1	40.6	40.6
5.417	2.523	2.523	1066	1066	51.2	51.2	38.6	38.6
9.239	3.671	3.671	1114	1114	47.8	47.8	37.1	37.1
18.315	6.205	6.205	1195	1195	45.7	45.7	36.8	36.8
20.147	8.037	8.037	1211	1211	45.3	45.3	36.7	36.7



Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

Flow profile

☒ Mass flow

☐ Funnel flow

Crit. values

☒ No (all)

☐ t = 0

☐ 4.00 h

☐ 8.00 h

☐ -

☐ -

☐ -

☐ -

☐ -

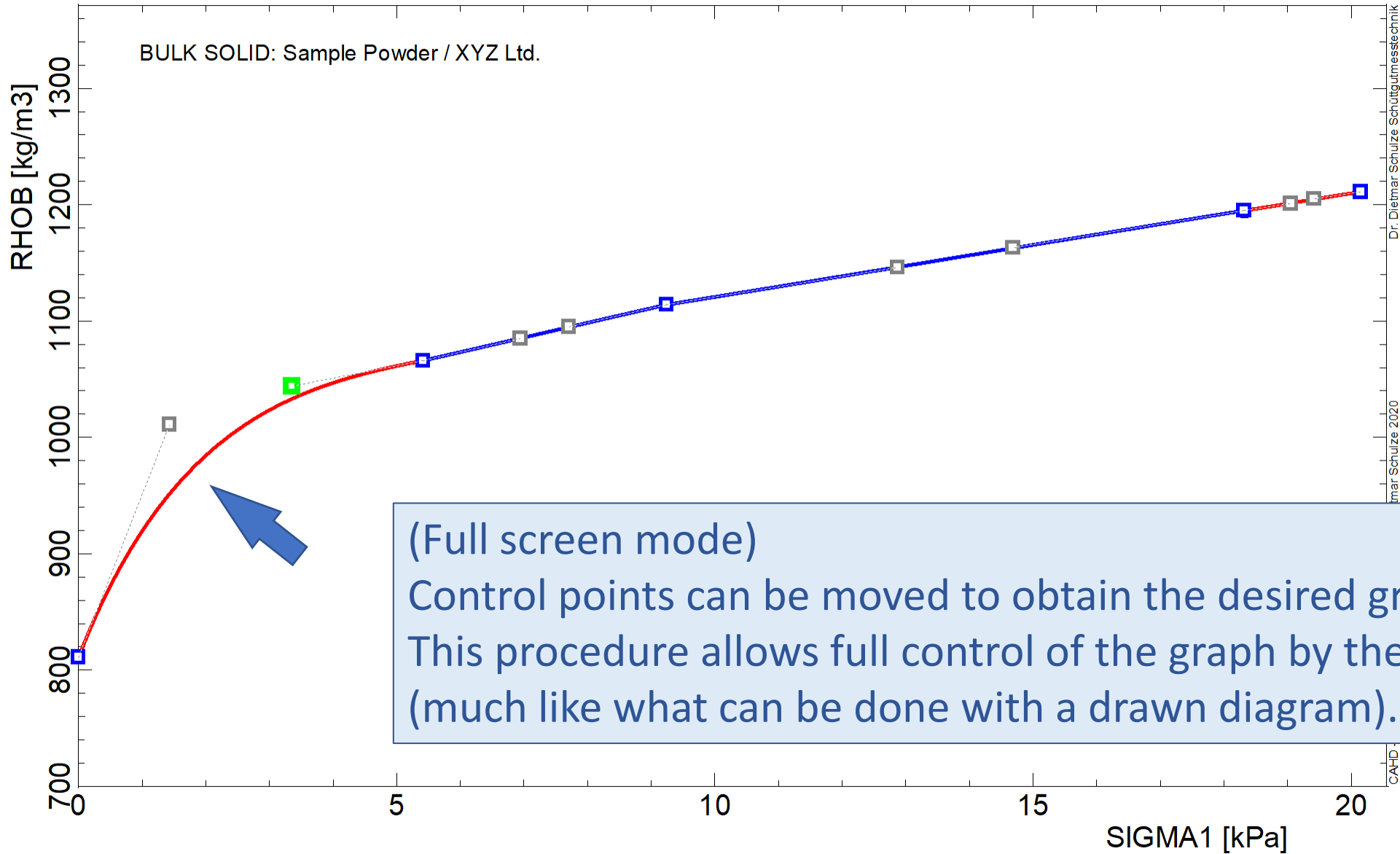
☐ -

☐ -

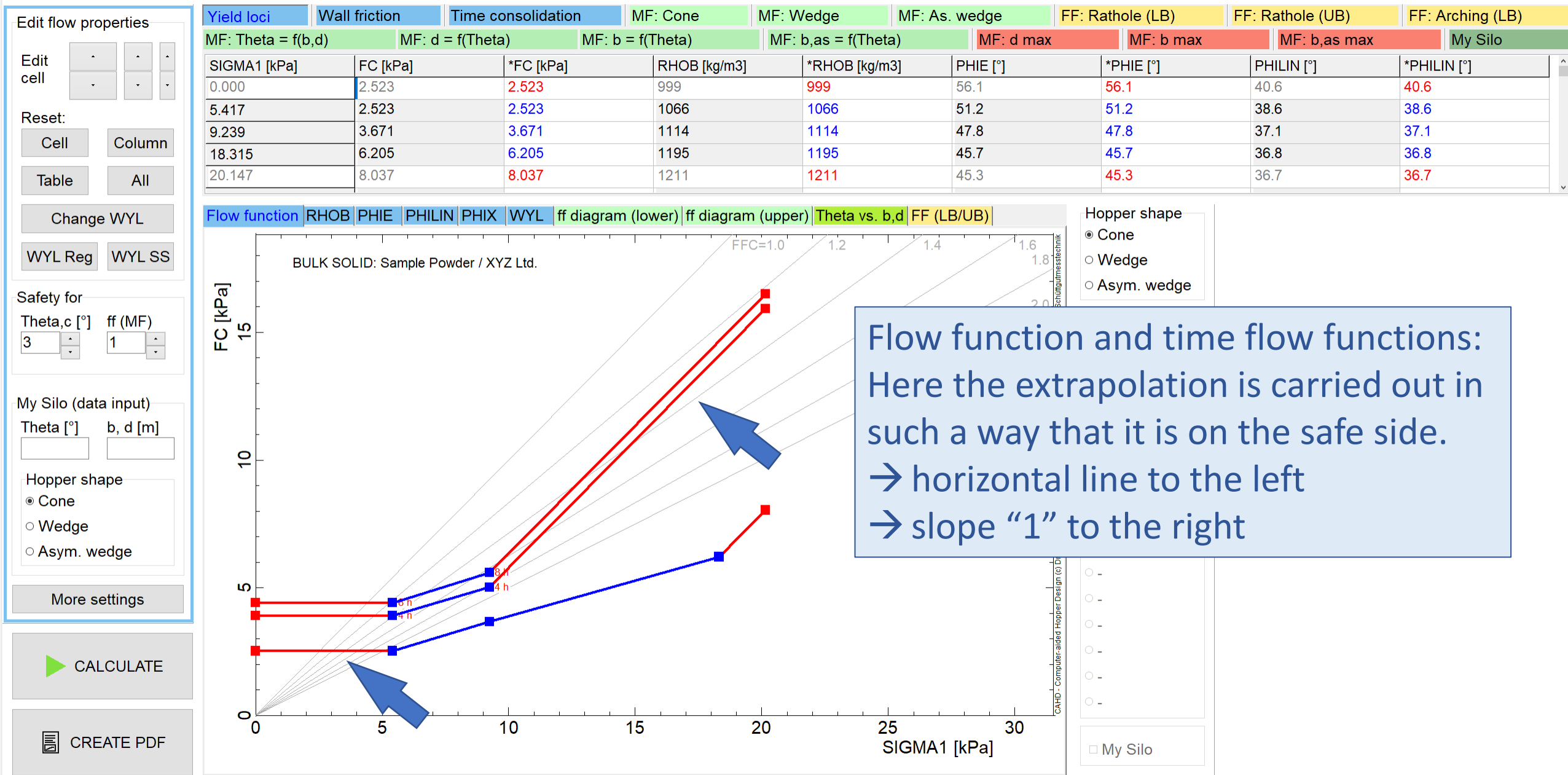
☐ -

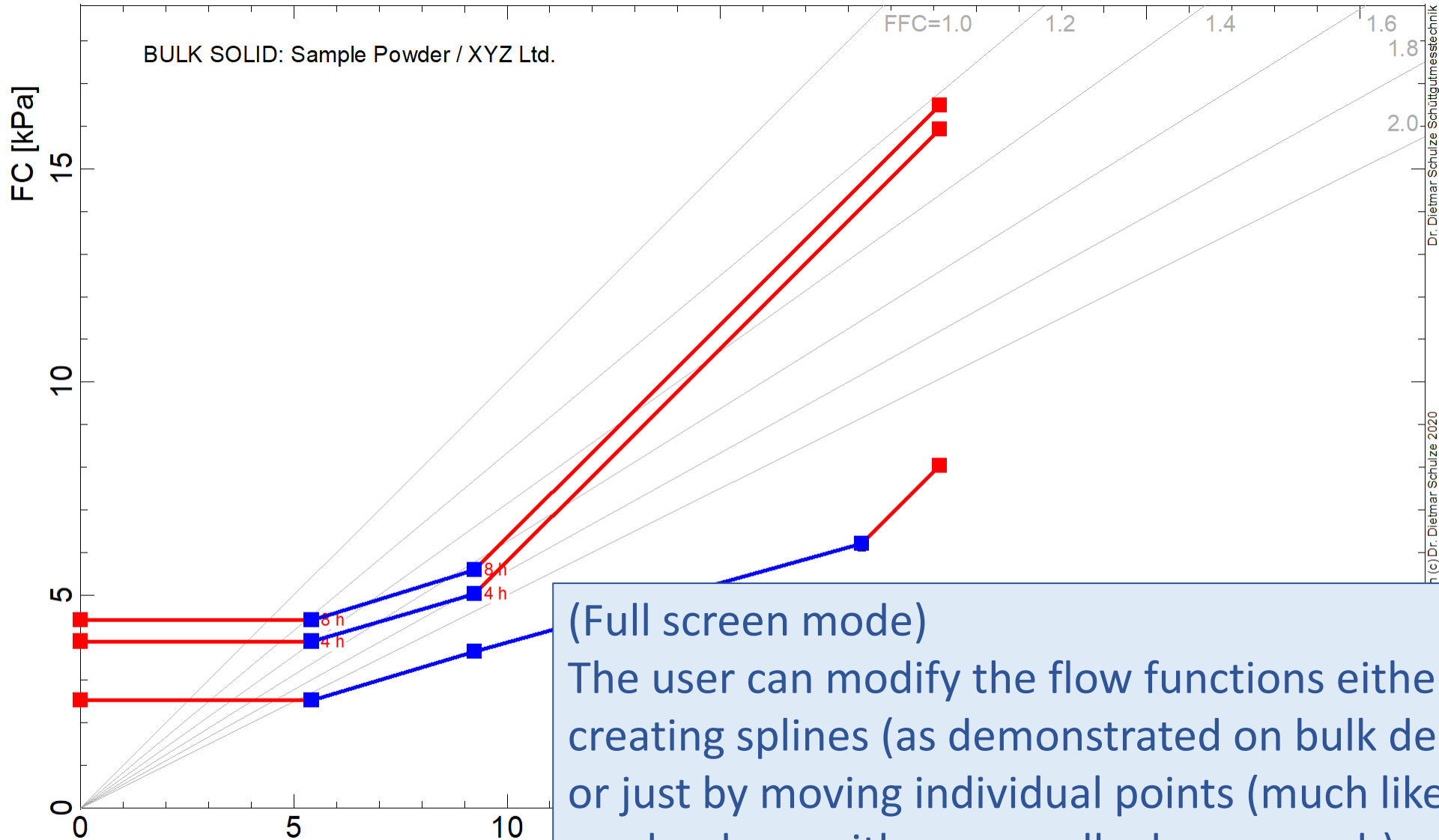
My Silo

SIGMA1 [kPa]: RHOB [kg/m3]: Error approx. RHOB [kg/m3]: Error approx. SIGMA1 [kPa]: Screen coordinates: [358;642]



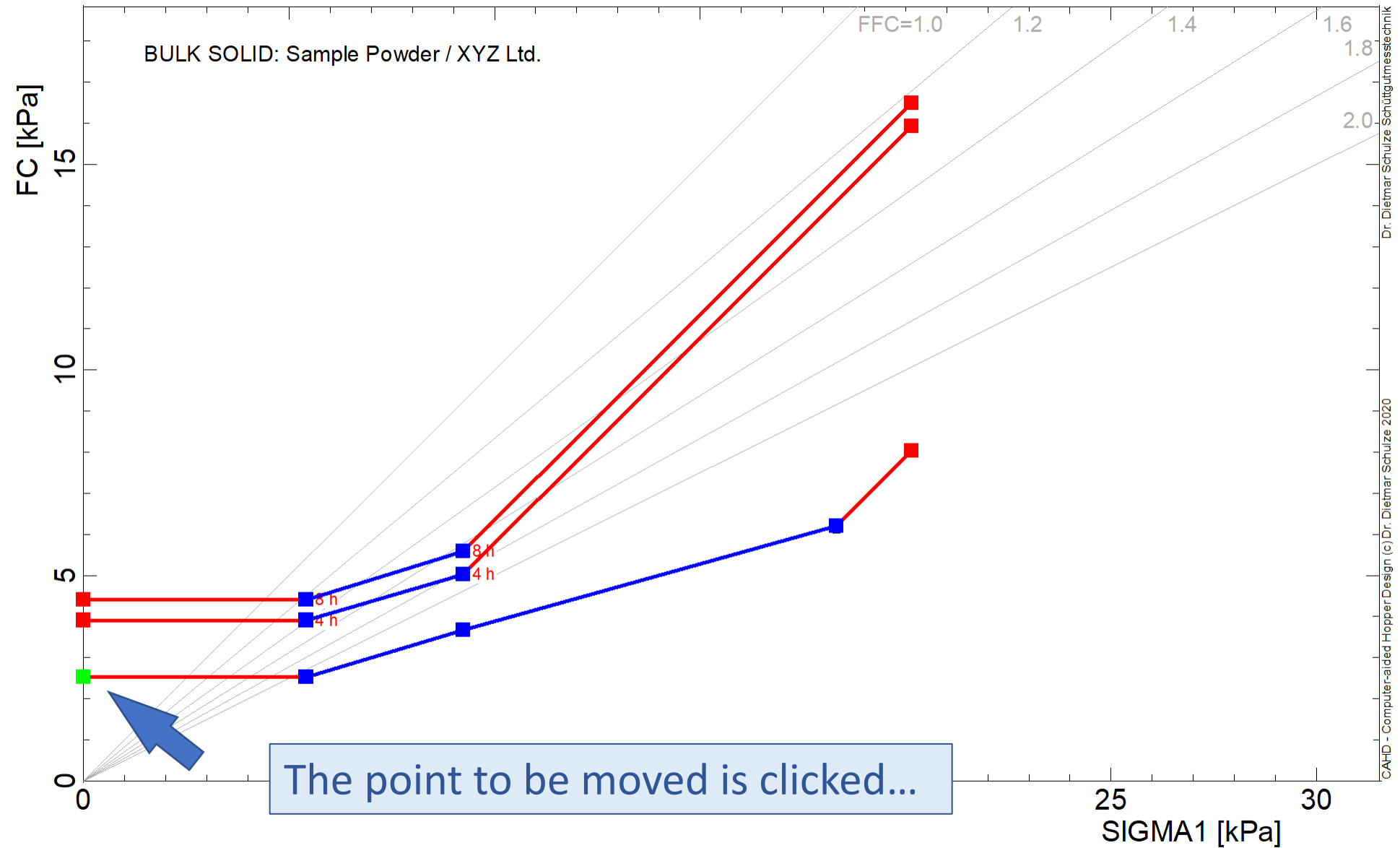
Close



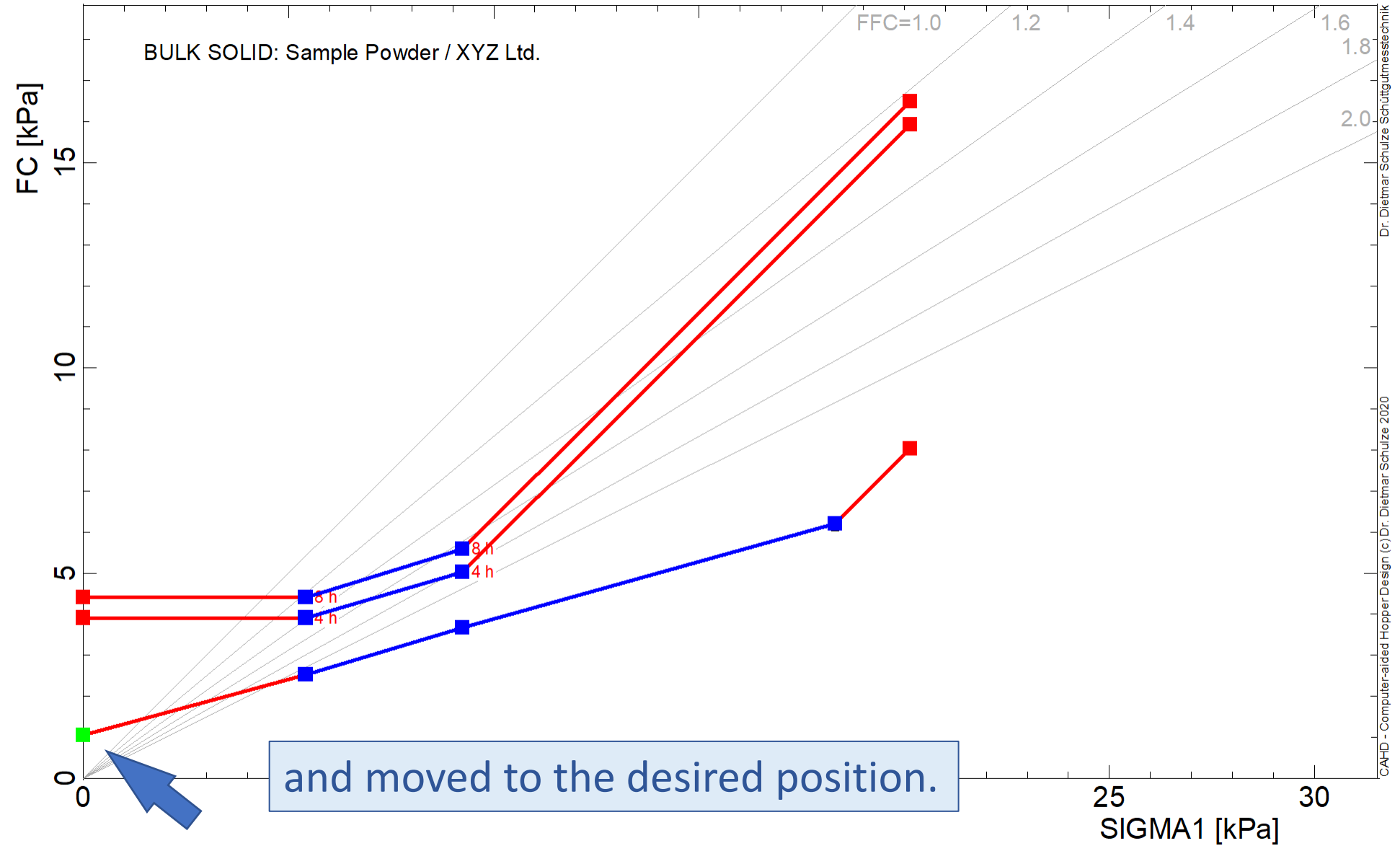


Zoom: Right click.

Close



Close



Close

SIGMA1 [kPa]: 11.542

FC [kPa]:

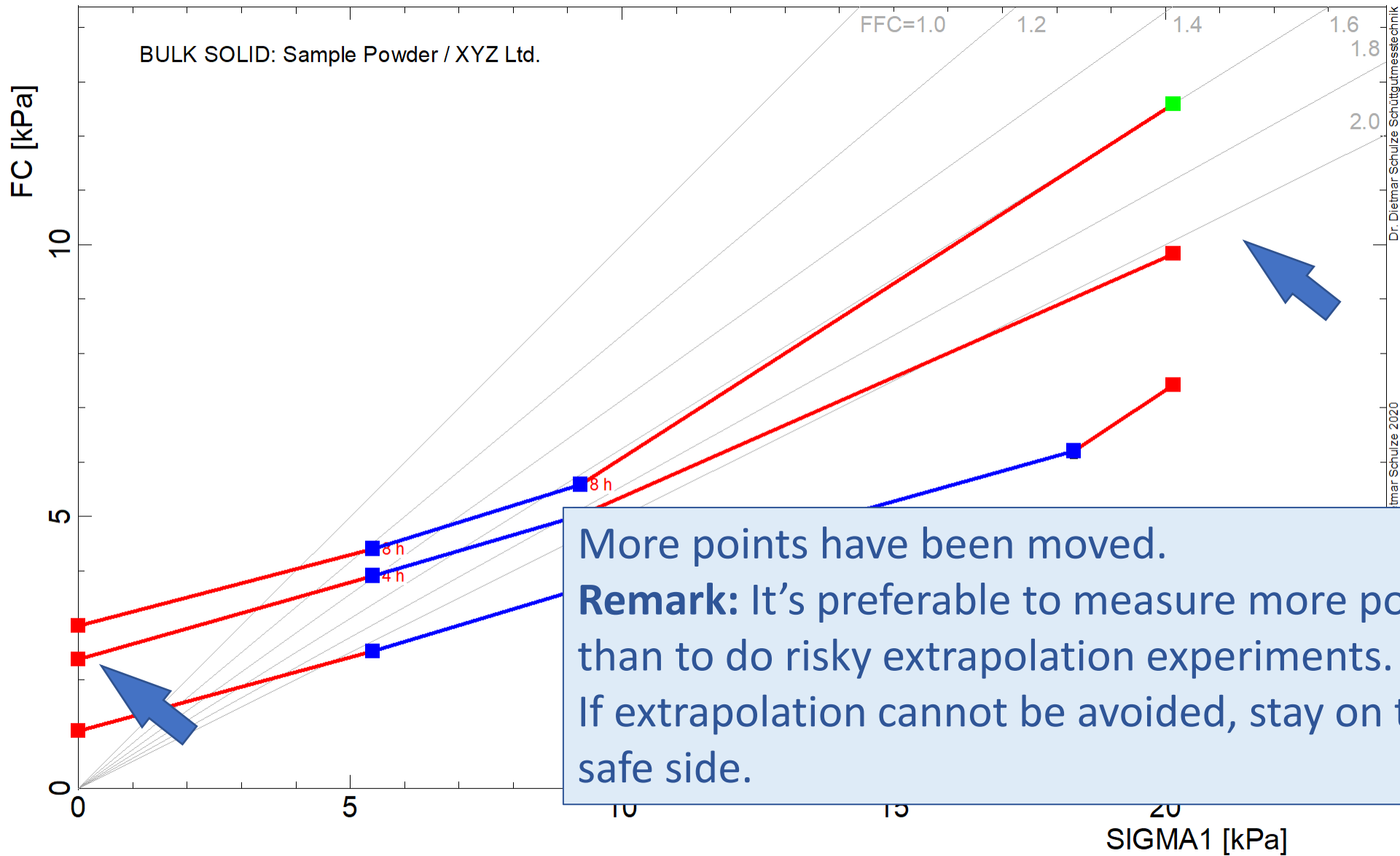
-2.833

Error approx. [kPa]:

0.0134

FFC = SIGMA1/FC:

Screen coordinates: [968;1407]



More points have been moved.

Remark: It's preferable to measure more points than to do risky extrapolation experiments. If extrapolation cannot be avoided, stay on the safe side.

Close

Edit cell

Reset:

Cell Column

Table All

Change WYL

WYL Reg WYL SS

Safety for

Theta, c [°] ff (MF)

3 1

My Silo (data input)

Theta [°]	b, d [m]

Hopper shape

- ☒ Cone
- ☐ Wedge
- ☐ Asym. wedge

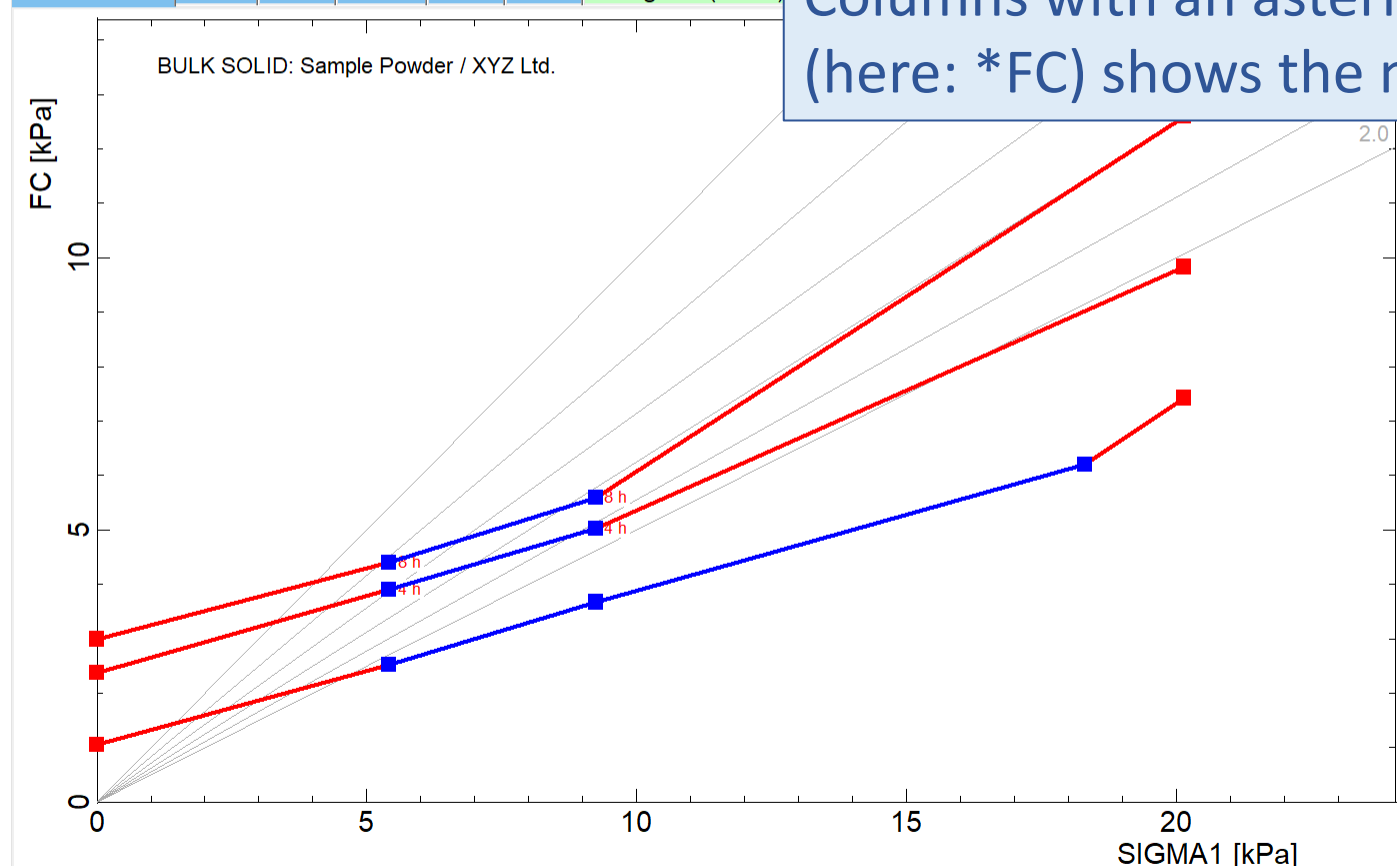
More settings

 CALCULATE

CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)	
MF: Theta = f(b,d)		MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo
SIGMA1 [kPa]	FC [kPa]	*FC [kPa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]	
0.000	2.523	1.055	811	811	56.1	56.1	40.6	40.6	
5.417	2.523	2.523	1066	1066	51.2	51.2	38.6	38.6	
9.239	3.671	3.671	1114	1114	47.8	47.8	37.1	37.1	
18.315	6.205	6.205	1195	1195	45.7	45.7	36.8	36.8	
20.147	8.037	7.421	1211	1211	45.3	45.3	36.7	36.7	

Flow function	RHOB	PHIE	PHILIN	PHIX	WYL	ff diagram (lower)
---------------	------	------	--------	------	-----	--------------------



Columns with an asterisk in the column header (here: *FC) shows the modified values.

- Flow profile
 - Mass flow
 - Funnel flow

Crit. values

☒ No (all)

○ $t = 0$

☐ 4.00 h

☐ 8.00 h

☐ My Silo

Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3.0

1

My Silo (data input)

Theta [°]

b, d [m]

Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

More settings

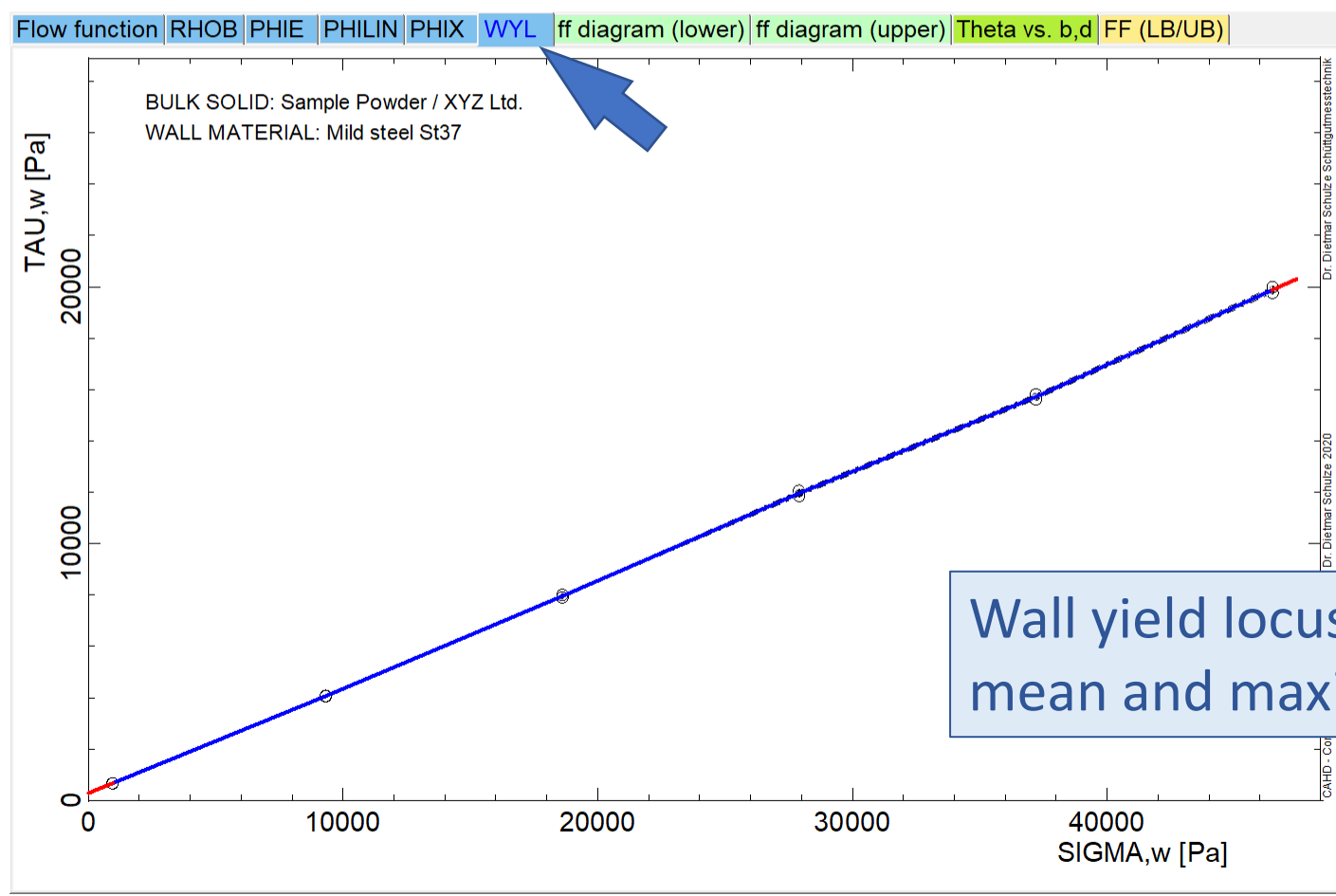
▶

CALCULATE

📄

CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
SIGMA,w [Pa]	PHIX,min [°]	PHIX,m [°]	PHIX,max [°]	*PHIX [°]	Vertical wall (asymm.)			
10	87.9	88.0	88.0	88.0	No entry: PHIXV = PHIX			
955	34.7	34.9	35.1	34.9	PHIXV [°]			
9320	23.5	23.6	23.6	23.6				
18613	23.0	23.1	23.3	23.1				
27907	23.0	23.2	23.4	23.2				



Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

Flow profile

☒ Mass flow

☐ Funnel flow

Crit. values

☒ No (all)

☐ t = 0

☐ 4.00 h

☐ 8.00 h

☐ -

☐ -

☐ -

☐ -

☐ My Silo

Wall yield locus and table with minimum, mean and maximum wall friction angles

Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3.0

1

My Silo (data input)

Theta [°]

b, d [m]

Hopper shape

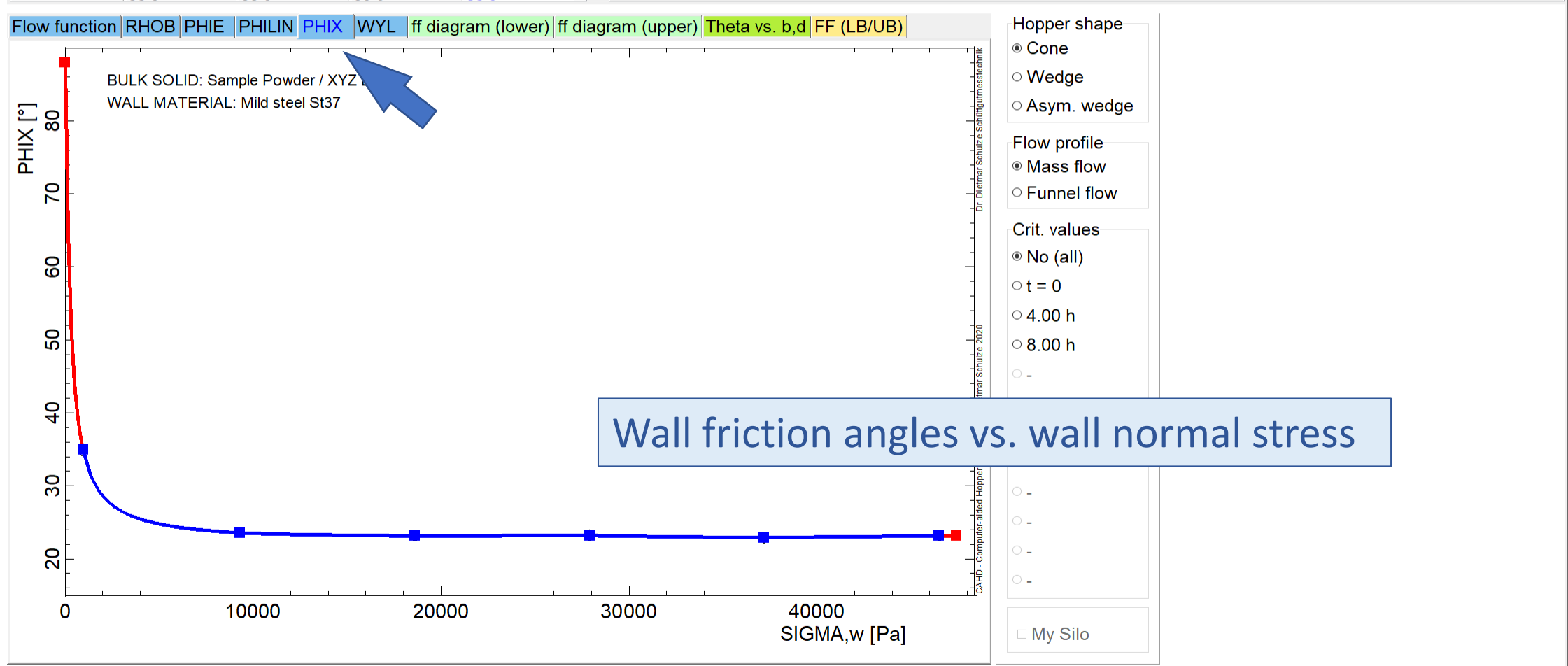
☒ Cone

☐ Wedge

☐ Asym. wedge

More settings

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
SIGMA,w [Pa]	PHIX,min [°]	PHIX,m [°]	PHIX,max [°]	*PHIX [°]	Vertical wall (asymm.)			
10	87.9	88.0	88.0	88.0	No entry: PHIXV = PHIX			
955	34.7	34.9	35.1	34.9	PHIXV [°]			
9320	23.5	23.6	23.6	23.6				
18613	23.0	23.1	23.3	23.1				
27907	23.0	23.2	23.4	23.2				



Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]ff (MF)

3.01

My Silo (data input)

Theta [°]b, d [m]

Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

More settings

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
SIGMA,w [Pa]	PHIX,min [°]	PHIX,m [°]	PHIX,max [°]	*PHIX [°]	Vertical wall (asymm.)			
10	87.9	88.0	88.0	88.0	No entry: PHIXV = PHIX			
955	34.7	34.9	35.1	34.9	PHIXV [°]			
9320	23.5	23.6	23.6	23.6				
18613	23.0	23.1	23.3	23.1				
27907	23.0	23.2	23.4	23.2				

Flow function

RHOB

PHIE

PHILIN

PHIX

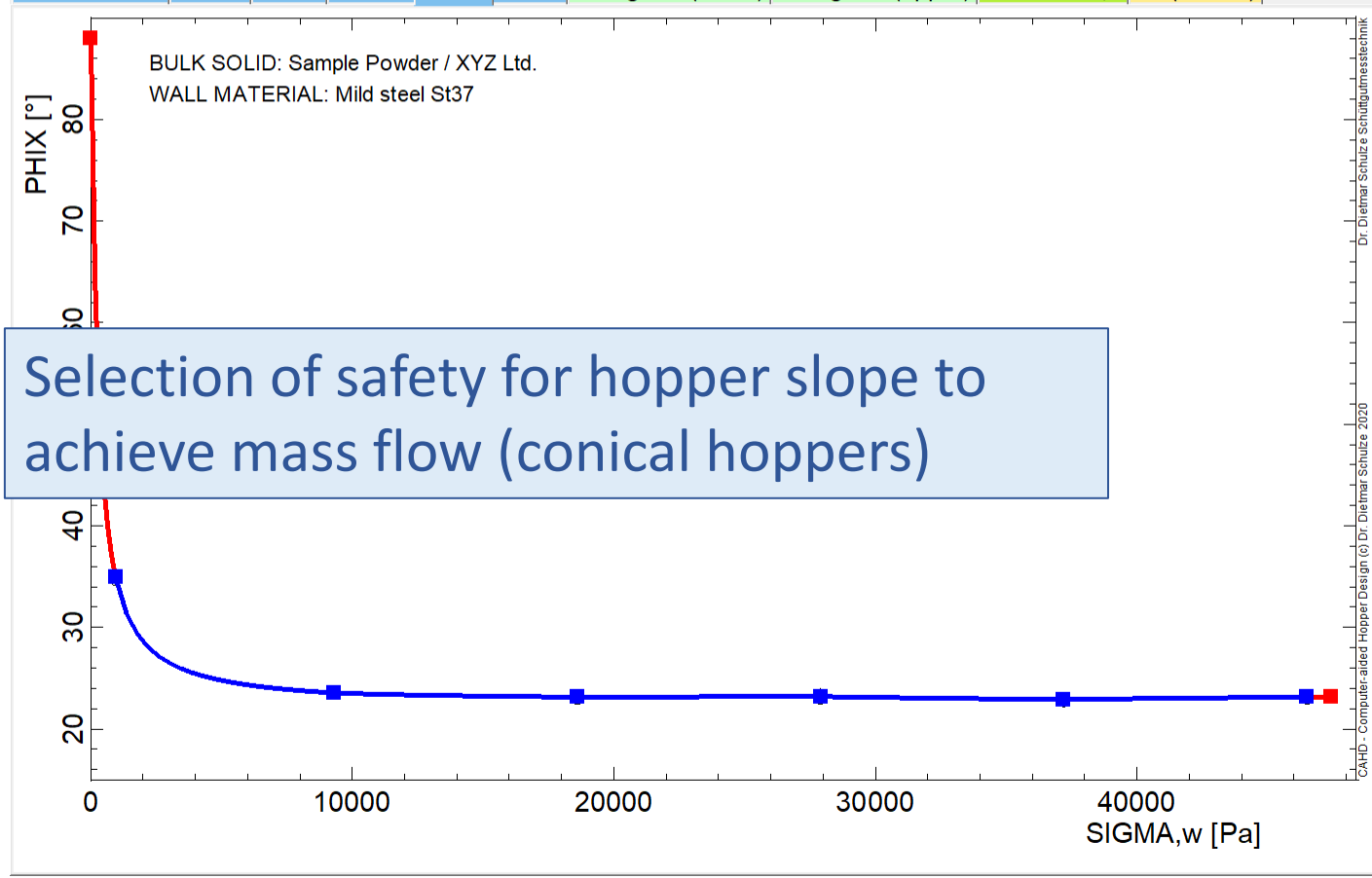
WYL

ff diagram (lower)

ff diagram (upper)

Theta vs. b,d

FF (LB/UB)



Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

Flow profile

☒ Mass flow

☐ Funnel flow

Crit. values

☒ No (all)

☐ t = 0

☐ 4.00 h

☐ 8.00 h

☐ -

☐ -

☐ -

☐ -

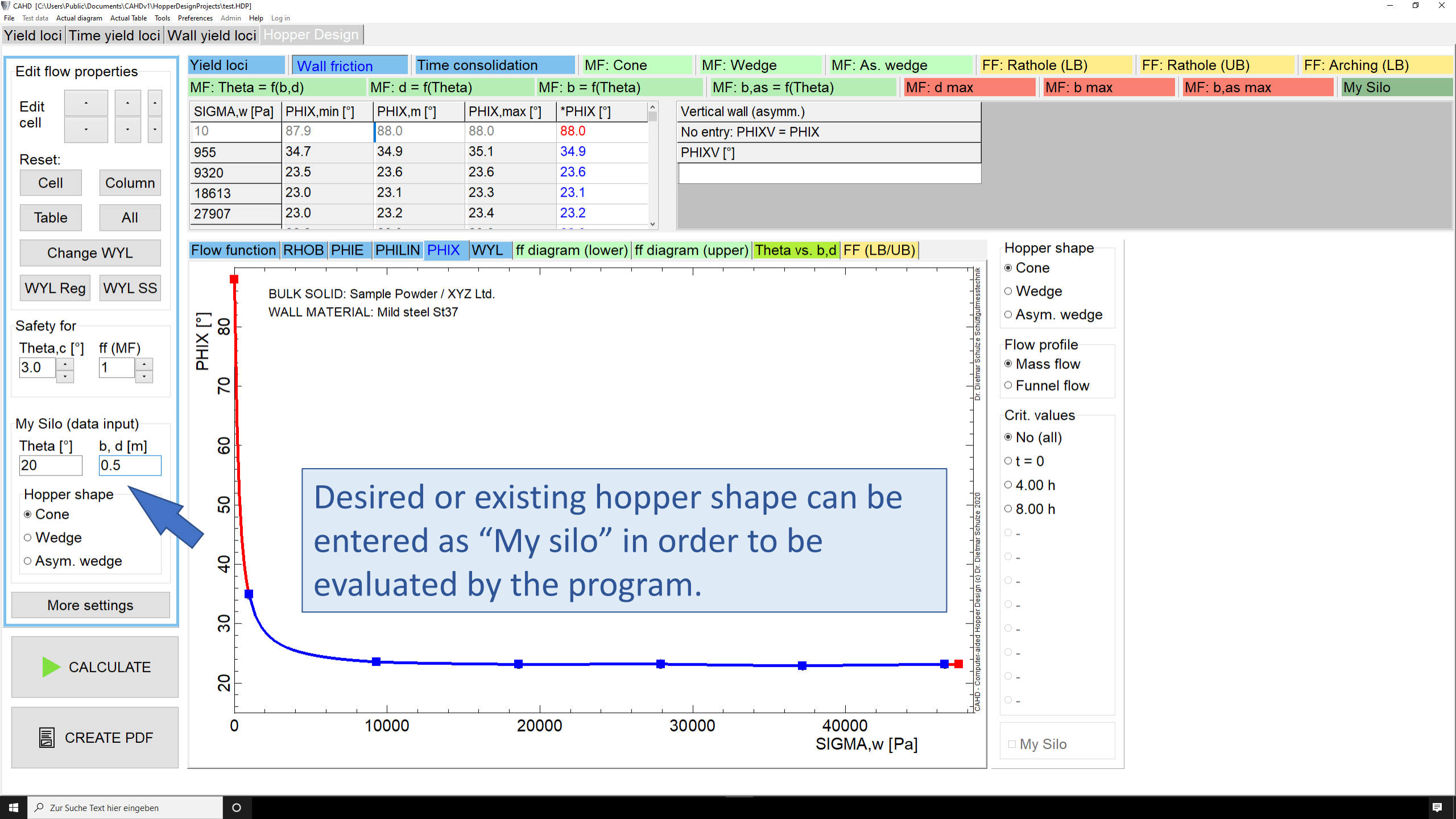
☐ -

☐ -

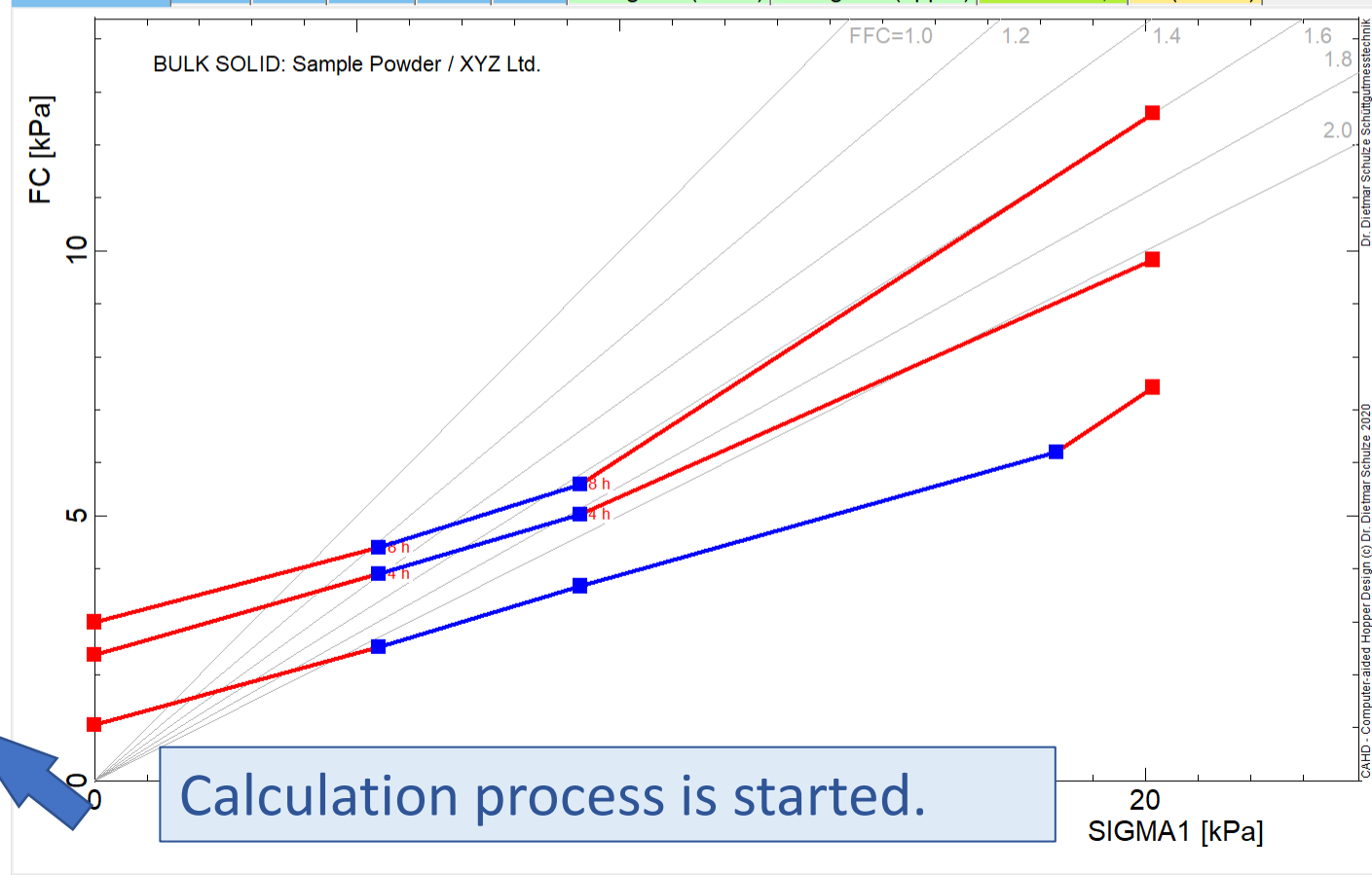
☐ -

☐ -

☐ My Silo



SIGMA1 [kPa]	FC [kPa]	*FC [kPa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]
0.000	2.523	1.055	811	811	56.1	56.1	40.6	40.6
5.417	2.523	2.523	1066	1066	51.2	51.2	38.6	38.6
9.239	3.671	3.671	1114	1114	47.8	47.8	37.1	37.1
18.315	6.205	6.205	1195	1195	45.7	45.7	36.8	36.8
20.147	8.037	7.421	1211	1211	45.3	45.3	36.7	36.7



Hopper shape

- ☒ Cone
- ☐ Wedge
- ☐ Asym. wedge

- Flow profile
 - Mass flow
 - Funnel flow

Crit. values

☒ No (all)

○ $t = 0$

☐ 4.00 h

☐ 8.00 h

☐

○

☐☐☐ My Silo

Edit flow properties

Edit cell

Reset:

Cell Column

Table All

Change WYL

WYL Reg WYL SS

Safety for

Theta, c [°]	ff (MF)
3	1

My Silo (data input)

Theta [°]	b, d [m]
20	0.5

Hopper shape

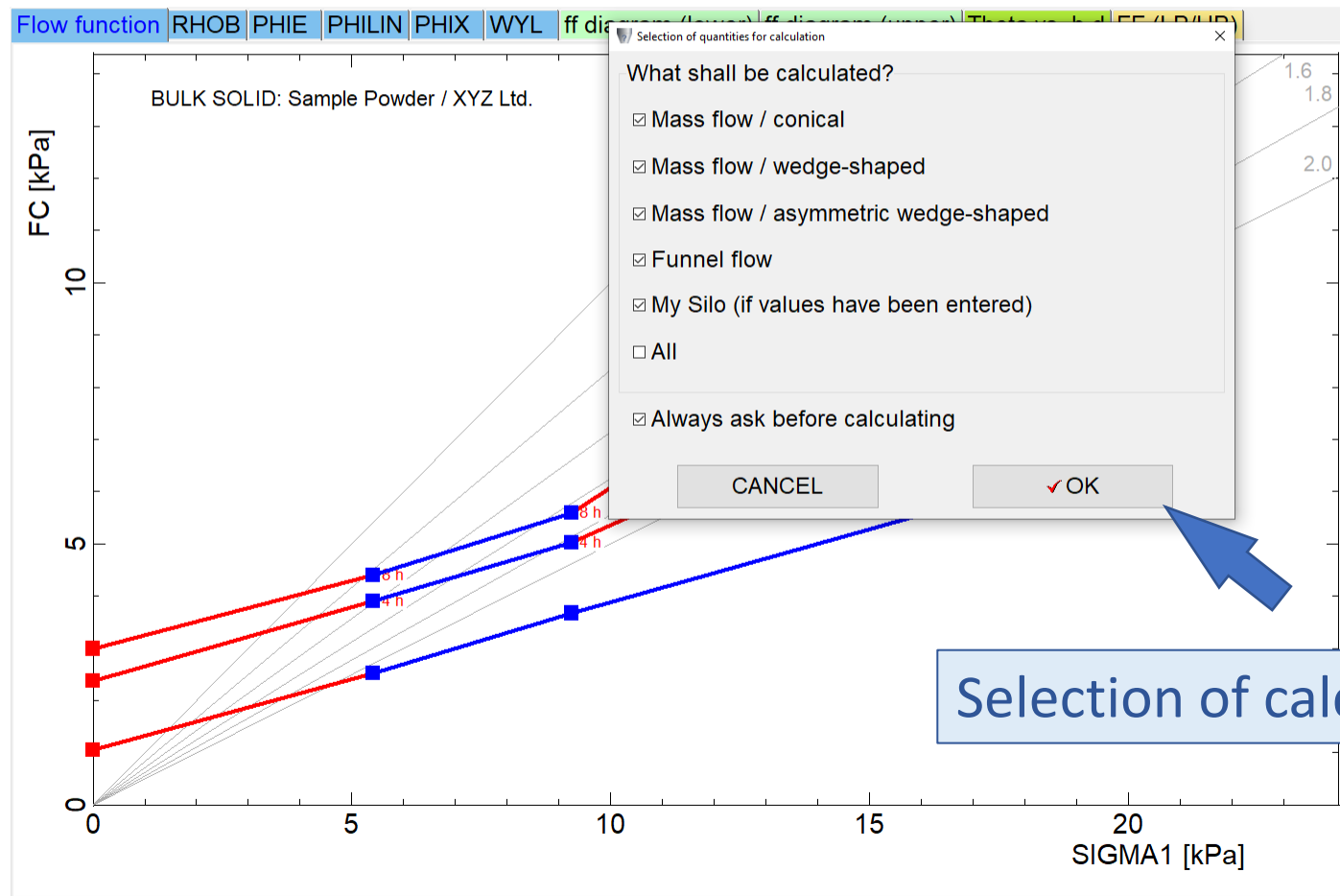
- ☒ Cone
- ☐ Wedge
- ☐ Asym. wedge

More settings

 CALCULATE

 CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)	
MF: Theta = f(b,d)		MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo
SIGMA1 [kPa]	FC [kPa]	*FC [kPa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]	
0.000	2.523	1.055	811	811	56.1	56.1	40.6	40.6	
5.417	2.523	2.523	1066	1066	51.2	51.2	38.6	38.6	
9.239	3.671	3.671	1114	1114	47.8	47.8	37.1	37.1	
18.315	6.205	6.205	1195	1195	45.7	45.7	36.8	36.8	
20.147	8.037	7.421	1211	1211	45.3	45.3	36.7	36.7	



Hopper shape

- ☒ Cone
- ☐ Wedge
- ☐ Asym. wedge

- Flow profile
 - Mass flow
 - Funnel flow

Crit. values

- ☒ No (all)
- ☐ $t = 0$
- ☐ 4.00 h
- ☐ 8.00 h

Simulation

☐ My Silo

Selection of calculations.

Edit cell

Reset:

Cell Column

Table All

Change WYL

WYL Reg WYL SS

Safety for

Theta, c [°]	ff (MF)
3	1

My Silo (data input)

Theta [°]	b, d [m]
20	0.5

Hopper shape

- Cone
- Wedge
- Asym. wedge

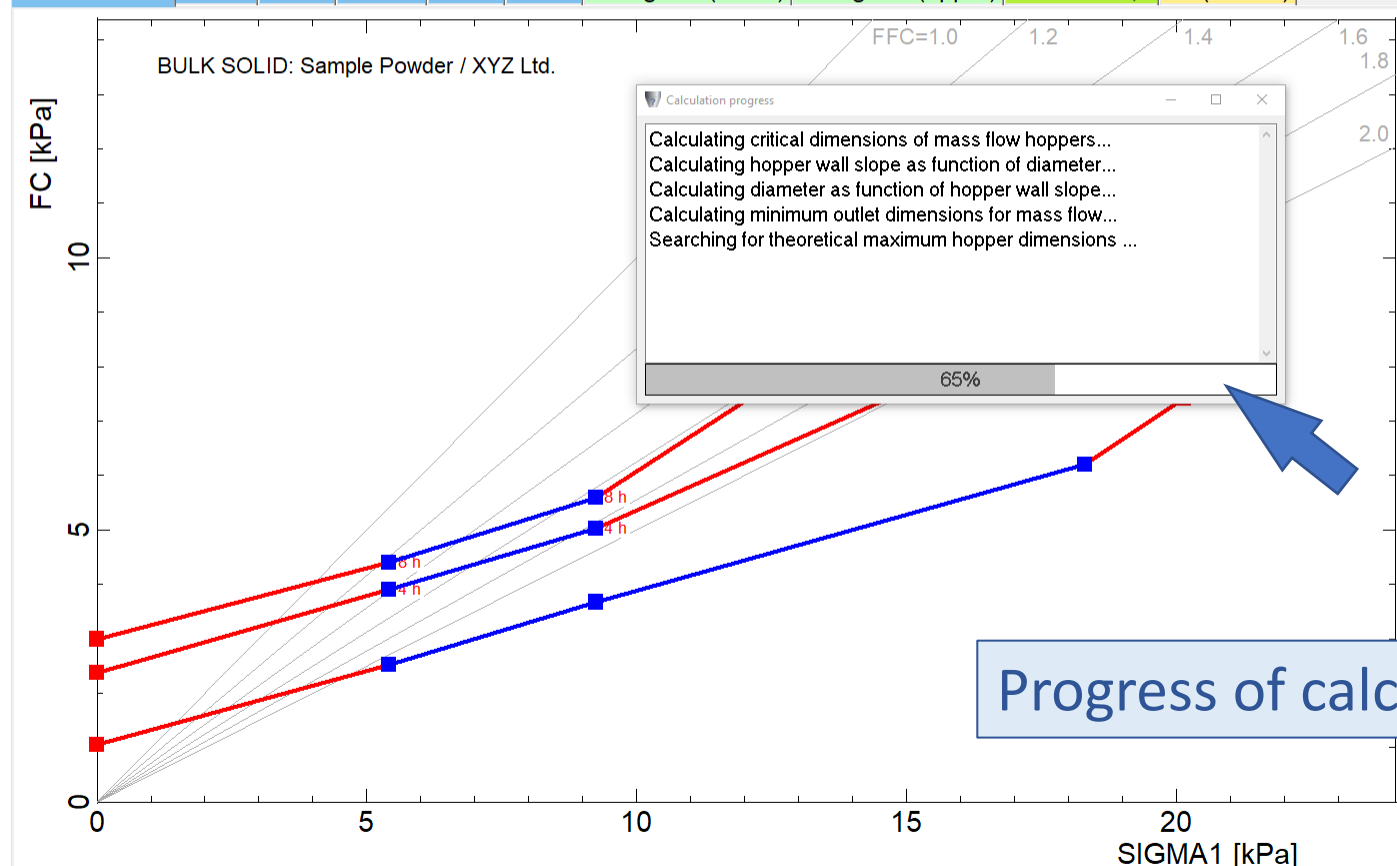
More settings

CALCULATE

CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)	
MF: Theta = f(b,d)		MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo
SIGMA1 [kPa]	FC [kPa]	*FC [kPa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]	
0.000	2.523	1.055	811	811	56.1	56.1	40.6	40.6	
5.417	2.523	2.523	1066	1066	51.2	51.2	38.6	38.6	
9.239	3.671	3.671	1114	1114	47.8	47.8	37.1	37.1	
18.315	6.205	6.205	1195	1195	45.7	45.7	36.8	36.8	
20.147	8.037	7.421	1211	1211	45.3	45.3	36.7	36.7	

Flow function	RHOB	PHIE	PHILIN	PHIX	WYL	ff diagram (lower)	ff diagram (upper)	Theta vs. b,d	FF (LB/UB)
---------------	------	------	--------	------	-----	--------------------	--------------------	---------------	------------



Hopper shape

- ☒ Cone
- ☐ Wedge
- ☐ Asym. wedge

Flow profile

- Mass flow
- Funnel flow

Crit. values

☒ No (all)
☐ $t = 0$
☐ 4.00 h
☐ 8.00 h
☐ -
☐ -
☐ -
☐ -

☐ My Silo

Progress of calculation process

Edit flow properties

Edit cell	▲	▲	▲
	▼	▼	▼

Reset:

Cell Column

Table All

Change WYL

WYL Reg WYL SS

Safety for

Theta, c [°] ff (MF)

3 1

My Silo (data input)

Theta [°]	b, d [m]
20	0.5

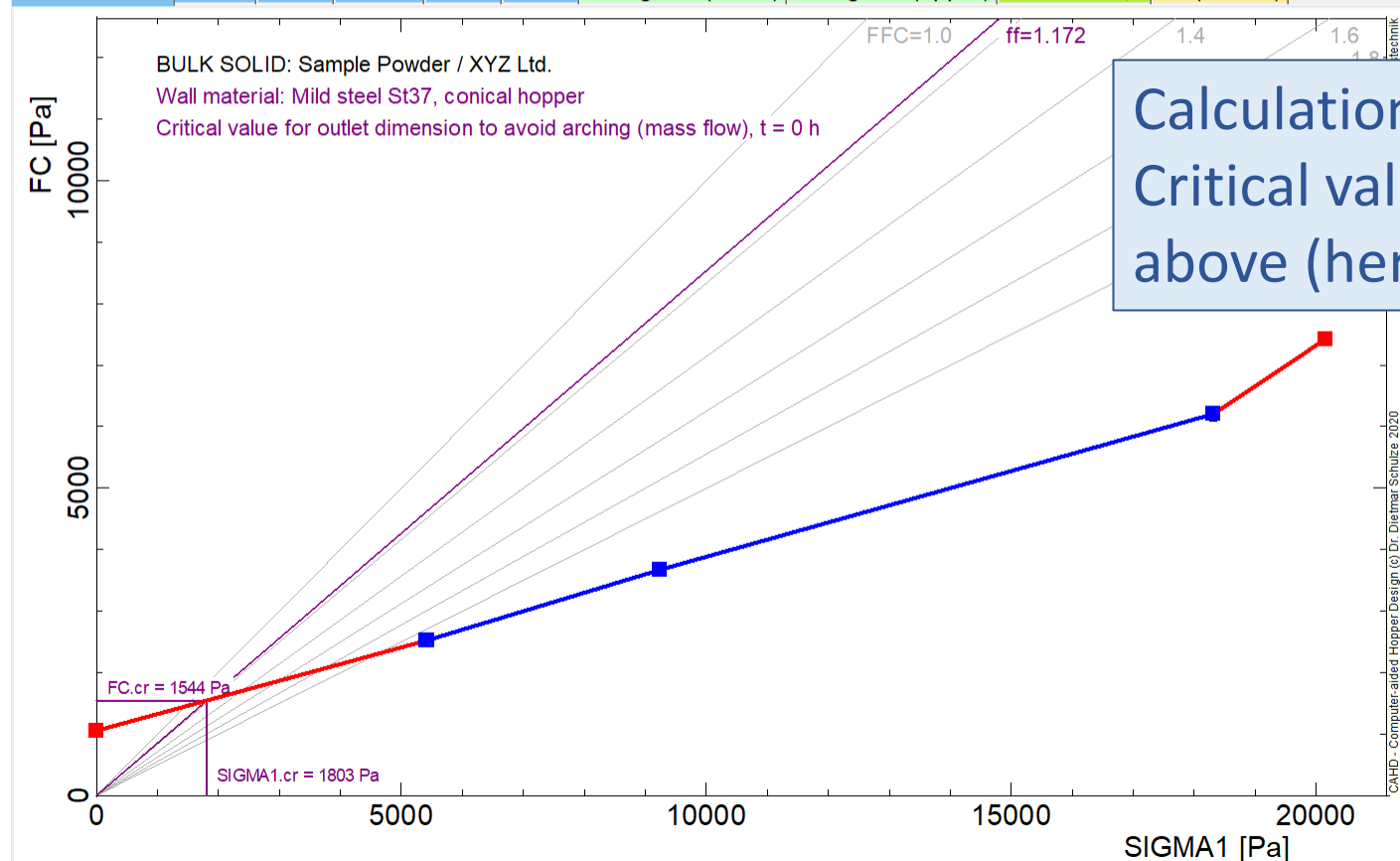
- Hopper shape
 - ☒ Cone
 - ☐ Wedge
 - ☐ Asym. wedge

More settings

 CALCULATE

 CREATE PDF[illegible]

Flow function	RHOB	PHIE	PHILIN	PHIX	WYL	ff diagram (lower)	ff diagram (upper)	Theta vs. b,d	FF (LB/UB)
---------------	------	------	--------	------	-----	--------------------	--------------------	---------------	------------



Calculation is done.
Critical values are given in the tables
above (here: conical hopper).

Hopper shape

- ☒ Cone
- ☐ Wedge

☐ No (all)

⊙ $t = 0$

1.00

☐ 4.00 h

☐ 8.00 h

 Springer[illegible]

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☐ ☒

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466
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☐ My Silo

Edit flow properties

Edit cell

↑

↓

↕

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

3

ff (MF)

1

My Silo (data input)

Theta [°]

20

b, d [m]

0.5

Hopper shape

☒ Cone

☐ Wedge

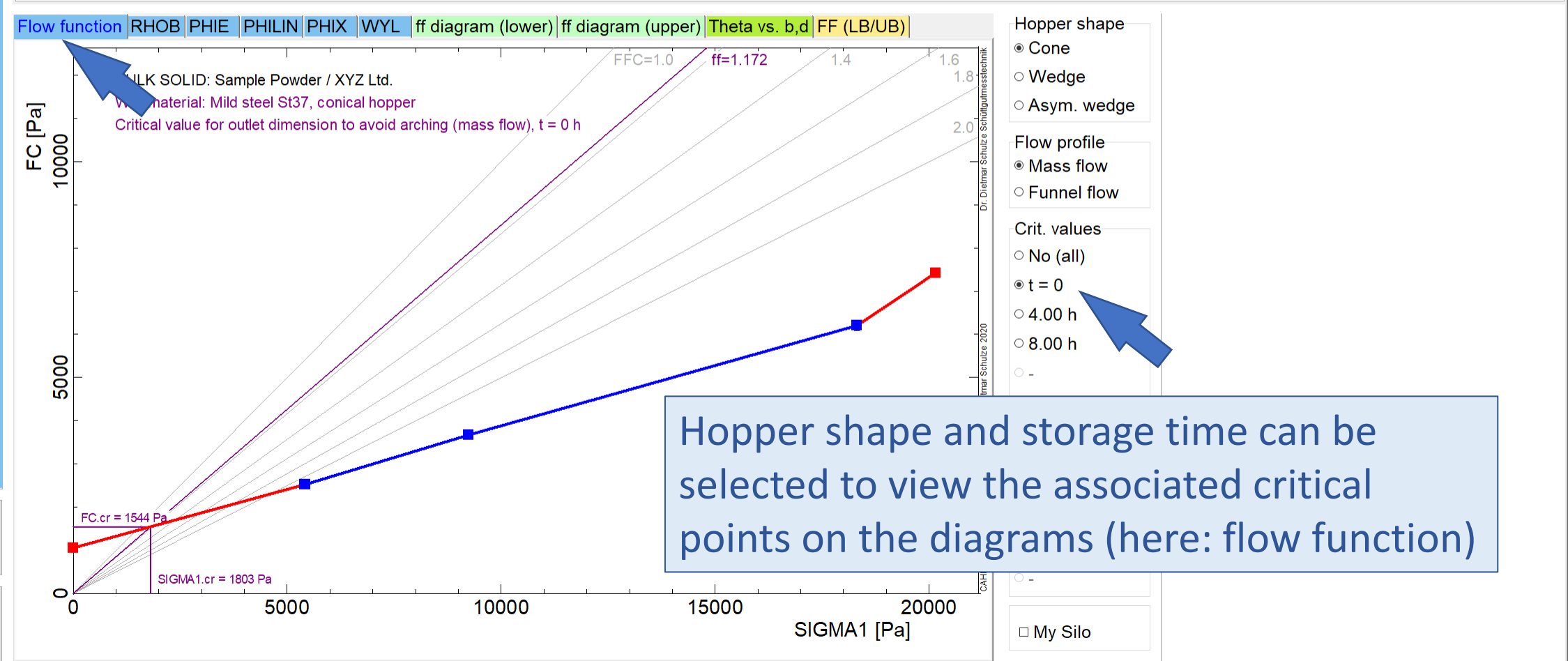
☐ Asym. wedge

More settings

CALCULATE

CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)						
MF: Theta = f(b,d)		MF: d = f(Theta)		MF: b = f(Theta)		MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo			
Time [h]	SIGMA1,cr [Pa]	SIGMAW,cr [Pa]	FC,cr [Pa]	RHOB,cr [kg/m3]	PHIE,cr [°]	PHIX,cr [°]	PHILIN,cr [°]	Theta,c [°]	ff [-]	H [-]	d,cr [m]	q [-]	SIGMAV,cr [Pa]	Comment
0	1803	1223	1544	975	54.4	32.4	39.9	8.5	1.172	2.13	0.344	0.145	608	
4.00	4564	3576	3666	1056	52.0	25.8	38.9	16.2	1.244	2.25	0.796	0.155	1626	
8.00	5634	4469	4471	1069	51.0	25.1	38.5	17.0	1.259	2.26	0.964	0.158	2033	



Hopper shape and storage time can be selected to view the associated critical points on the diagrams (here: flow function)

Edit flow properties

Edit cell

↑

↓

↕

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

20

0.5

Hopper shape

☒ Cone

☐ Wedge

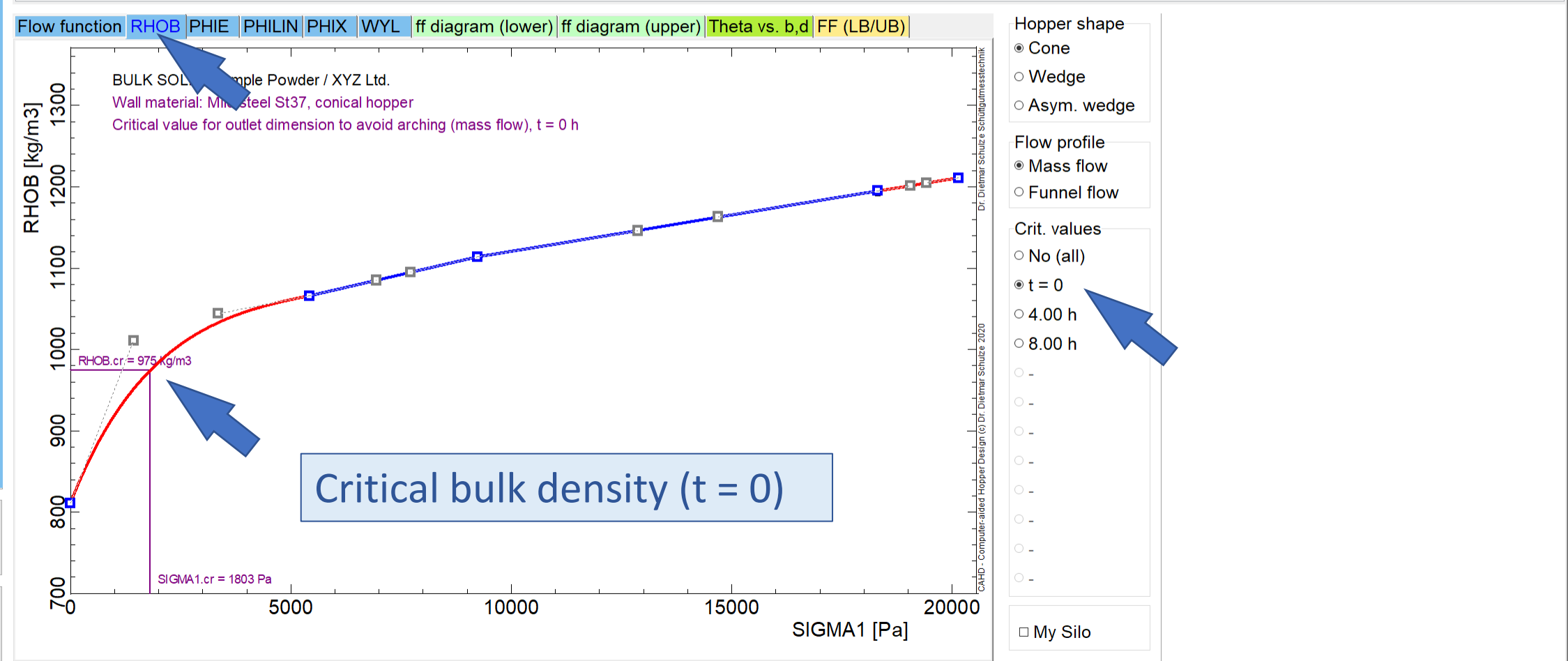
☐ Asym. wedge

More settings

CALCULATE

CREATE PDF

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)						
MF: Theta = f(b,d)		MF: d = f(Theta)		MF: b = f(Theta)		MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo			
Time [h]	SIGMA1,cr [Pa]	SIGMAW,cr [Pa]	FC,cr [Pa]	RHOB,cr [kg/m3]	PHIE,cr [°]	PHIX,cr [°]	PHILIN,cr [°]	Theta,c [°]	ff [-]	H [-]	d,cr [m]	q [-]	SIGMAV,cr [Pa]	Comment
0	1803	1223	1544	975	54.4	32.4	39.9	8.5	1.172	2.13	0.344	0.145	608	
4.00	4564	3576	3666	1056	52.0	25.8	38.9	16.2	1.244	2.25	0.796	0.155	1626	
8.00	5634	4469	4471	1069	51.0	25.1	38.5	17.0	1.259	2.26	0.964	0.158	2033	



Edit flow properties

Edit cell

↑

↓

↕

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

3

ff (MF)

1

My Silo (data input)

Theta [°]

20

b, d [m]

0.5

Hopper shape

☒ Cone

☐ Wedge

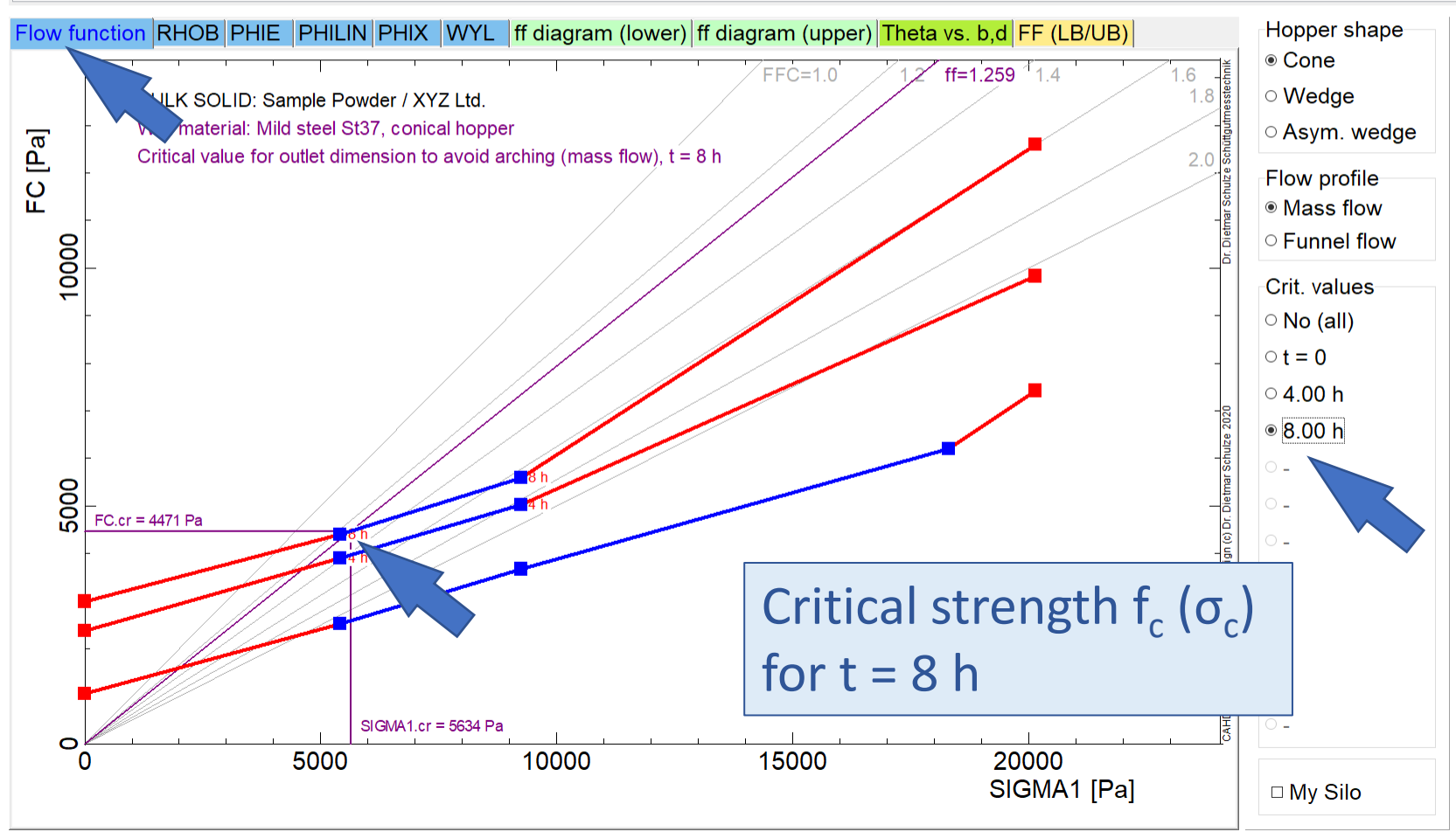
☐ Asym. wedge

More settings

CALCULATE

CREATE PDF

Yield loci		Wall friction		Time consolidation		MF: Cone		MF: Wedge		MF: As. wedge		FF: Rathole (LB)		FF: Rathole (UB)		FF: Arching (LB)			
MF: Theta = f(b,d)			MF: d = f(Theta)			MF: b = f(Theta)			MF: b,as = f(Theta)			MF: d max		MF: b max		MF: b,as max		My Silo	
Time [h]	SIGMA1,cr [Pa]	SIGMAW,cr [Pa]	FC,cr [Pa]	RHOB,cr [kg/m3]	PHIE,cr [°]	PHIX,cr [°]	PHILIN,cr [°]	Theta,c [°]	ff [-]	H [-]	d,cr [m]	q [-]	SIGMAV,cr [Pa]	Comment					
0	1803	1223	1544	975	54.4	32.4	39.9	8.5	1.172	2.13	0.344	0.145	608						
4.00	4564	3576	3666	1056	52.0	25.8	38.9	16.2	1.244	2.25	0.796	0.155	1626						
8.00	5634	4469	4471	1069	51.0	25.1	38.5	17.0	1.259	2.26	0.964	0.158	2033						



Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

My Silo (data input)

Theta [°]

b, d [m]

Hopper shape

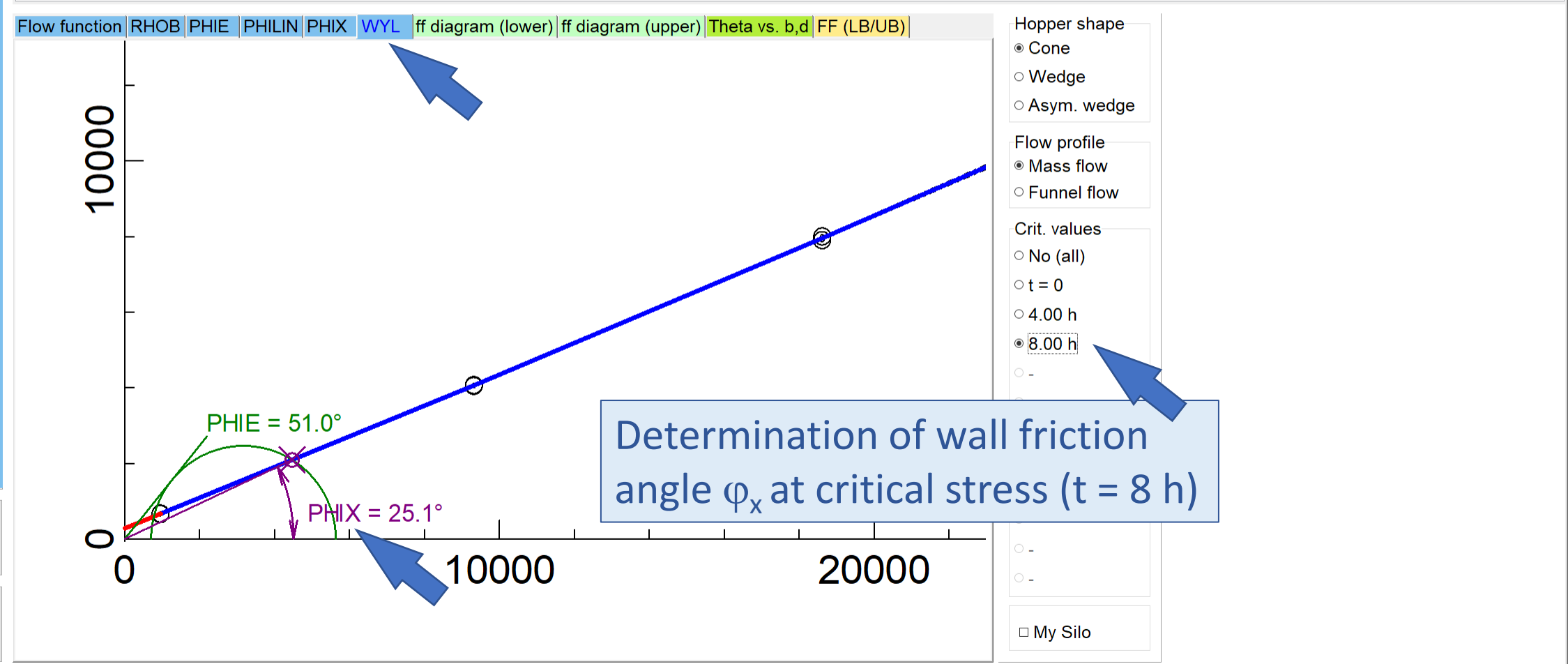
☒ Cone

☐ Wedge

☐ Asym. wedge

More settings

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)						
MF: Theta = f(b,d)		MF: d = f(Theta)		MF: b = f(Theta)		MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo			
Time [h]	SIGMA1,cr [Pa]	SIGMAW,cr [Pa]	FC,cr [Pa]	RHOB,cr [kg/m3]	PHIE,cr [°]	PHIX,cr [°]	PHILIN,cr [°]	Theta,c [°]	ff [-]	H [-]	d,cr [m]	q [-]	SIGMAV,cr [Pa]	Comment
0	1803	1223	1544	975	54.4	32.4	39.9	8.5	1.172	2.13	0.344	0.145	608	
4.00	4564	3576	3666	1056	52.0	25.8	38.9	16.2	1.244	2.25	0.796	0.155	1626	
8.00	5634	4469	4471	1069	51.0	25.1	38.5	17.0	1.259	2.26	0.964	0.158	2033	



Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

20

0.5

Hopper shape

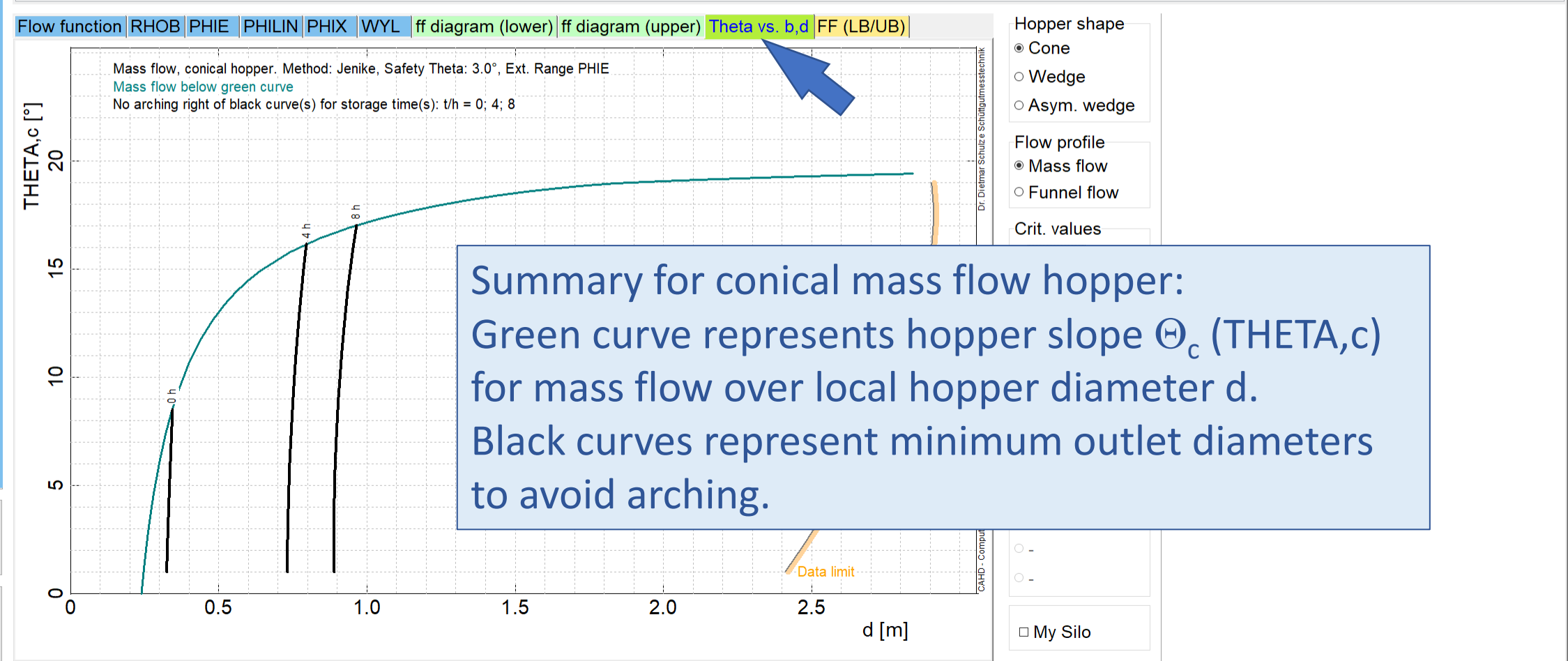
☒ Cone

☐ Wedge

☐ Asym. wedge

More settings

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)						
MF: Theta = f(b,d)		MF: d = f(Theta)		MF: b = f(Theta)		MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo			
Time [h]	SIGMA1,cr [Pa]	SIGMAW,cr [Pa]	FC,cr [Pa]	RHOB,cr [kg/m3]	PHIE,cr [°]	PHIX,cr [°]	PHILIN,cr [°]	Theta,c [°]	ff [-]	H [-]	d,cr [m]	q [-]	SIGMAV,cr [Pa]	Comment
0	1803	1223	1544	975	54.4	32.4	39.9	8.5	1.172	2.13	0.344	0.145	608	
4.00	4564	3576	3666	1056	52.0	25.8	38.9	16.2	1.244	2.25	0.796	0.155	1626	
8.00	5634	4469	4471	1069	51.0	25.1	38.5	17.0	1.259	2.26	0.964	0.158	2033	



Edit flow properties

Edit cell

▲

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Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta, c [°]

ff (MF)

3

▲

▼

1

▲

▼

My Silo (data input)

Theta [°]

b, d [m]

20

0.5

Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

More settings

Two buttons are shown. The top button is light gray with a green right-pointing triangle icon and the text 'CALCULATE'. The bottom button is also light gray with a document icon and the text 'CREATE PDF'.

Yield loci	Wall friction	Time consolidation			MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)	
MF: Theta = f(b,d)		MF: d = f(Theta)			MF: b = f(Theta)	MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo
Theta,c [°] t [h]	0	4.00	8.00	Unit							Comment
19.0	1.848	1.848	1.848	m							Green: Minimum dimension for mass flow
18.0	1.253	1.253	1.253	m							Green: Minimum dimension for mass flow
17.0	0.954	0.954	0.964	m							Green: Minimum dimension for mass flow
16.0	0.768	0.794	0.953	m							Green: Minimum dimension for mass flow
15.0	0.646	0.786	0.944	m							Green: Minimum dimension for mass flow

Flow function	RHOB	PHIE	PHILIN	PHIX	WYL	ff diagram (lower
---------------	------	------	--------	------	-----	-------------------

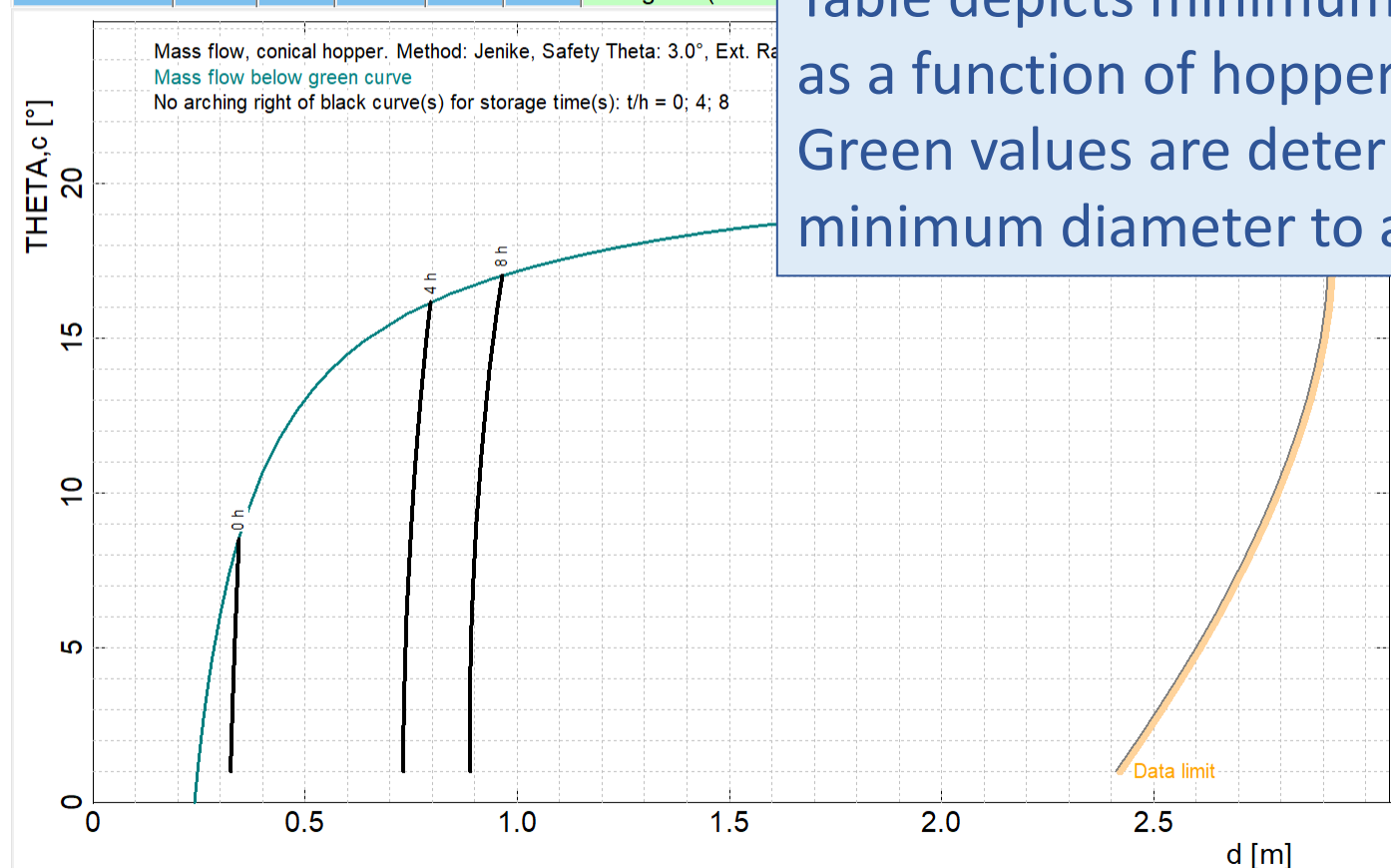


Table depicts minimum outlet diameter, d , as a function of hopper slope, Θ_c (THETA,c). Green values are determined by the minimum diameter to achieve mass flow.

☒ No (all)
☐ $t = 0$
☐ 4.00 h
☐ 8.00 h
☐ -
☐ -
☐ -
☐ -
☐ -
☐ -
☐ -
☐ -

☐ My Silo



Edit flow properties

Edit cell

Reset:

Cell Column

Table All

Change WYL

WYL Reg WYL SS

Safety for

Theta, c [°] ff (MF)

3 1

My Silo (data input)

Theta [°] b, d [m]

20 0.5

Hopper shape

☒ Cone

☐ Wedge

☐ Asym.

More

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
Theta, c [°] t [h]	0	4.00	8.00	Unit				Comment
19.0	1.848	1.848	1.848	m				Green: Minimum dimension for mass flow
18.0	1.253	1.253	1.253	m				Green: Minimum dimension for mass flow
17.0	0.954	0.954	0.964	m				Green: Minimum dimension for mass flow
16.0	0.768	0.794	0.953	m				Green: Minimum dimension for mass flow
15.0	0.646	0.786	0.944	m				Green: Minimum dimension for mass flow

Flow function RHOB PHIE PHILIN PHIX WYL ff diagram (lower) ff diagram (upper) Theta vs. b,d FF (LB/UB)



Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

Flow profile

☒ Mass flow

☐ Funnel flow

Crit. values

☒ No (all)

☐ t = 0

☐ 4.00 h

☐ 8.00 h

☐ -

☐ -

☐ -

☐ -

☐ -

☐ -

☐ -

☐ -

☐ My Silo

After all entries, modifications and results are checked and accepted, a report (pdf) can be created.

CREATE PDF

Edit flow properties

Edit cell

▲

▼

▲

▼

▲

▼

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta, c [°]

ff (MF)

3

▲

▼

1

▲

▼

My Silo (data input)

Theta [°]

b, d [m]

20

0.5

Hopper shape

☒ Cone

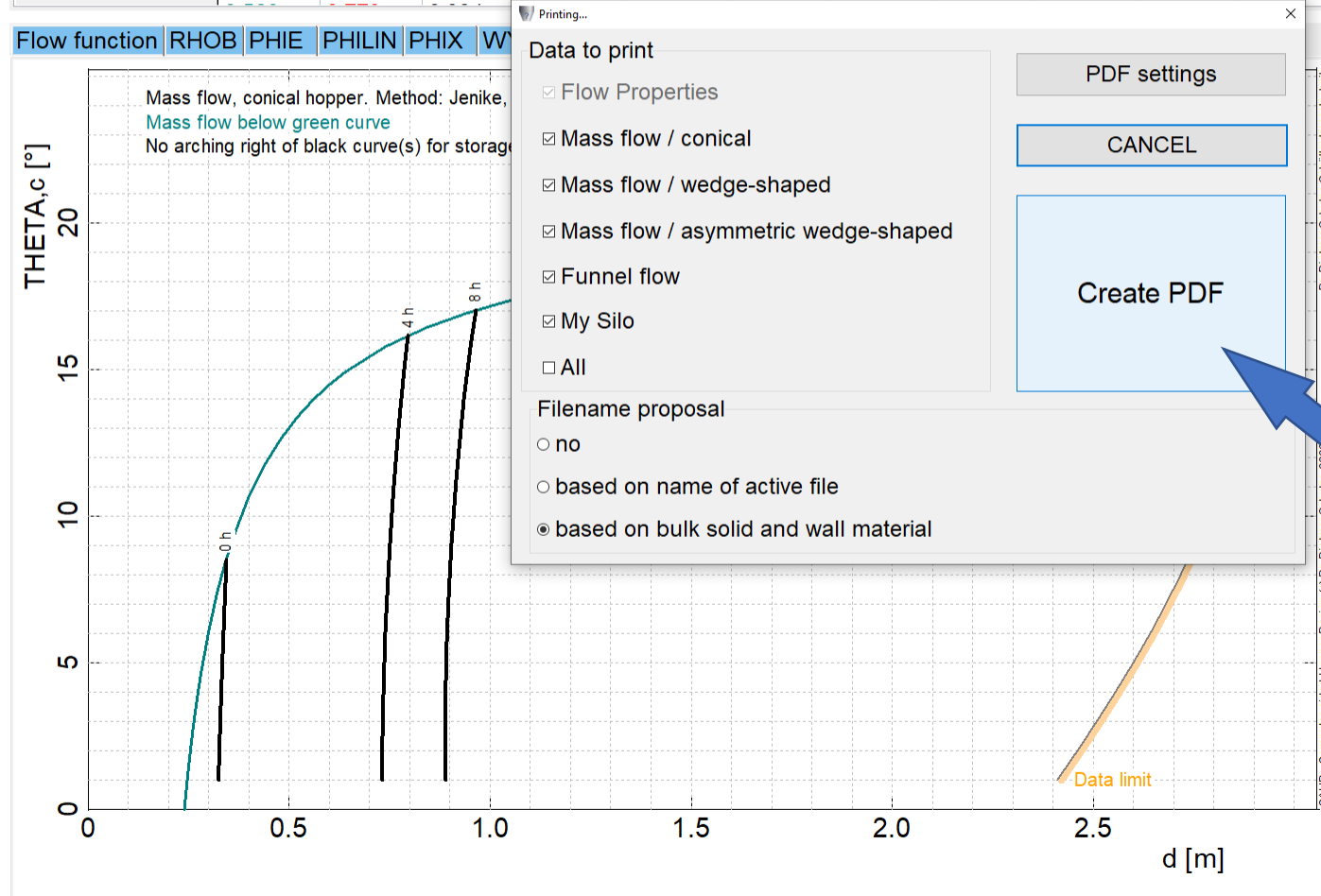
☐ Wedge

☐ Asym. wedge

More settings

CALCULATE
CREATE PDF

Yield loci	Wall friction	Time consolidation			MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)		
MF: Theta = f(b,d)		MF: d = f(Theta)		MF: b = f(Theta)			MF: b,as = f(Theta)		MF: d max	MF: b max	MF: b,as max	My Silo
Theta,c [°] t [h]	0	4.00	8.00	Unit								Comment
19.0	1.848	1.848	1.848	m								Green: Minimum dimension for mass flow
18.0	1.253	1.253	1.253	m								Green: Minimum dimension for mass flow
17.0	0.954	0.954	0.964	m								Green: Minimum dimension for mass flow
16.0	0.768	0.794	0.953	m								Green: Minimum dimension for mass flow
15.0	0.646	0.786	0.944	m								Green: Minimum dimension for mass flow



CAHD - Computer-aided Hopper Design (c) Dr. Dietmar Schülze 2022

Hopper shape

- ☒ Cone
- ☐ Wedge
- ☐ Asym. wedge

Flow profile

- ☒ Mass flow
- ☐ Funnel flow

Crit. values

- ☒ No (all)
- ☐ $t = 0$
- ☐ 4.00 h
- ☐ {
- ☐ Select
- ☐ includ
- ☐ -
- ☐ -
- ☐ -
- ☐ -

☐ My Silo

Selection of results to be included in the report

Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

My Silo (data input)

Theta [°]

b, d [m]

Hopper shape

More settings

Yield loci	Wall friction	Time consolidation	MF: Cone	MF: Wedge	MF: As. wedge	FF: Rathole (LB)	FF: Rathole (UB)	FF: Arching (LB)
MF: Theta = f(b,d)	MF: d = f(Theta)	MF: b = f(Theta)	MF: b,as = f(Theta)	MF: d max	MF: b max	MF: b,as max	My Silo	
Theta,c [°] t [h]	0	4.00	8.00	Unit				Comment
19.0	1.848	1.848	1.848	m				Green: Minimum dimension for mass flow
18.0	1.253	1.253	1.253	m				Green: Minimum dimension for mass flow
17.0	0.954	0.954	0.964	m				Green: Minimum dimension for mass flow
16.0	0.768	0.794	0.953	m				Green: Minimum dimension for mass flow
15.0	0.646	0.786	0.944	m				Green: Minimum dimension for mass flow

Flow function RHOB PHIE PHILIN PHIX W



Printing...

Printing PDF document ...

Page 5 of 26

CANCEL

19%

Hopper shape

Flow profile

Crit. values

My Silo

Progress of pdf printing process

Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

20

0.5

Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

More settings

CALCULATE

CREATE PDF

Yield loci	Wall friction	Time
MF: Theta = f(b,d)		MF: d = f(Theta)
Theta,c [°] t [h]	0	4.00
19.0	1.848	1.848
18.0	1.253	1.253
17.0	0.954	0.954
16.0	0.768	0.794
15.0	0.646	0.786

Flow function

RHOB

PHIE

PHILIN

P

Mass flow, conical hopper. Method
Mass flow below green curve
No arching right of black curve(s)

Sample Powder_Mild steel St37.pdf - Adobe Acrobat Reader DC

Datei Bearbeiten Anzeige Unterschreiben Fenster Hilfe

Start Werkzeuge Sample Powder_Mil... x

CAHD v1.0.0.9 Computer-aided Hopper Design - Software by Dr. Dietmar Schulze
File: C:\Users\Public\Documents\CAHDv1\Reports\Sample Powder_Mild steel St37.pdf

21.01.2021 16:26:46 page 1

Silo Design for Flow

Bulk solid:
Sample Powder

Wall material:
Mild steel St37

Order:
XYZ Ltd.

Design created by: unknown
21.01.2021

Title page of report

Zur Suche Text hier eingeben

Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

20

0.5

Hopper shape

☒ Cone

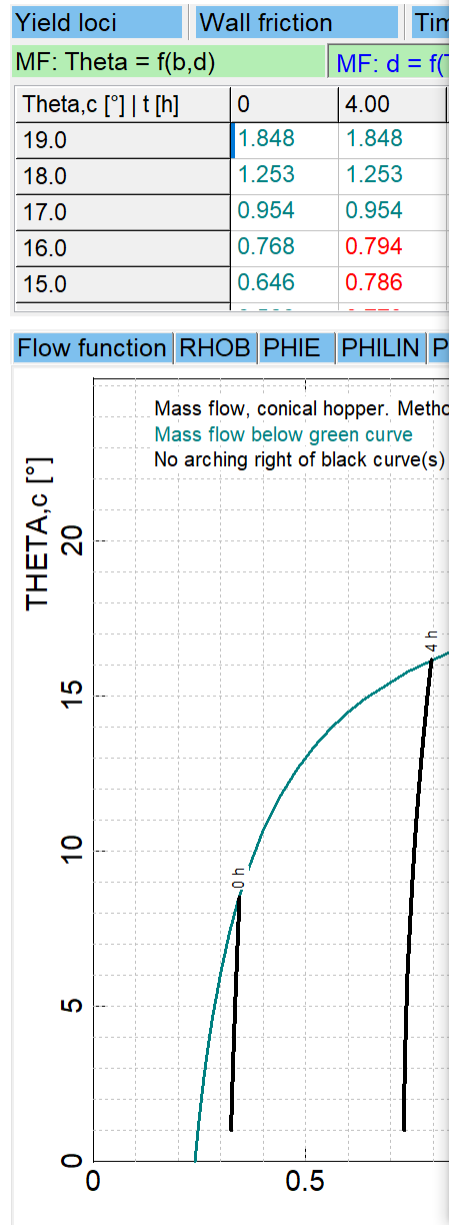
☐ Wedge

☐ Asym. wedge

More settings

CALCULATE

CREATE PDF



Sample Powder_Mild steel St37.pdf - Adobe Acrobat Reader DC

Datei Bearbeiten Anzeige Unterschreiben Fenster Hilfe

Start Werkzeuge Sample Powder_Mil... x

2 / 26 91%

CAHD v1.0.0.9 User: unknown 21.01.2021 16:26:46 page 2

Bulk solid: Sample Powder, Order: XYZ Ltd., Wall material: Mild steel St37

Flow properties for the design procedure

Test data: black
Data extrapolated by the program: purple
Extrapolated data, possibly modified by user: red
Data applied on design procedure, possibly modified by user: blue and **
The following functions are based on a user defined spline approximation:
RHOB

Flow properties derived from yield loci

SIGMA1 [Pa]	FC [Pa]	*FC [Pa]	RHOB [kg/m3]	*RHOB [kg/m3]	PHIE [°]	*PHIE [°]	PHILIN [°]	*PHILIN [°]
0	2523	1055	811	811	56.1	56.1	40.6	40.6
5417	2523	2523	1066	1066	51.2	51.2	38.6	38.6
9239	3671	3671	1114	1114	47.8	47.8	37.1	37.1
18315	6205	6205	1195	1195	45.7	45.7	36.8	36.8
20147	8037	7421	1211	1211	45.3	45.3	36.7	36.7

Wall friction (Mild steel St37)

SIGMA,w [Pa]	PHIX,min [°]	PHIX,m [°]	PHIX,max [°]	*PHIX [°]
10	87.9	85.0	85.0	85.0
955	34.7	34.9	35.1	34.9
9320	23.5	23.6	23.6	23.6
18613	23.0	23.1	23.3	23.1
27907	23.0	23.2	23.4	23.2
37200	22.8	22.9	23.0	22.9
46494	23.0	23.2	23.3	23.2
47423	23.1	23.2	23.3	23.2

Time consolidation:

SIGMA1 [Pa]	4.00	*4.00	8.00	Storage time t [h]
0	3907	2374	4404	2990
5417	3907	2374	4404	4404
9239	5025	5025	5587	5587
18315				
20147	15932	9831	16495	12592

Important note - Disclaimer (Program CAHD):

The silo design results presented on the following pages are based on the above quantities printed in blue and red color. This data may be incorrect, and/or may have been modified by the user.
For the calculations the design procedures selected by the user were applied. Alone the user is responsible for the correctness of the silo design results. Thus, the user must be sufficiently educated in the silo design procedure. Extrapolation, interpolation, and all calculations of the program have to be regarded as proposals which have to be reviewed critically and may require modification by the user in order to obtain a reliable silo design.
Thus, the originator of this program does not take any responsibility for silo design results of this program.

The user shall accept and understand that no warranty and liability is expressed or implied by the originator of this program on the accuracy and reliability of this program. Should the program prove defective, the originator shall bear no responsibility for all resulting damages or losses.
By using this program, the user agrees to the terms above, and to the terms and conditions written in the manual of this program.

Flow properties and possible modifications by the user

Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

20

0.5

Hopper shape

☒ Cone

☐ Wedge

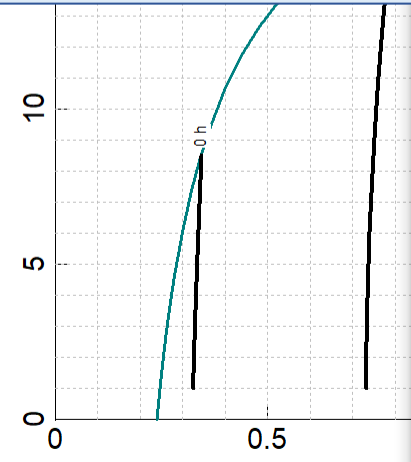
☐ Asym. wedge

More settings

Yield loci		Wall friction		Time	
MF: Theta = f(b,d)		MF: d = f(			
Theta,c [°] t [h]	0	4.00			
19.0	1.848	1.848			
18.0	1.253	1.253			
17.0	0.954	0.954			
16.0	0.768	0.794			
15.0	0.646	0.786			

Results for conical hopper:

- critical points for all storage times t
- d = f(Theta)
- Theta = f(d)



Design of conical hopper (mass flow, arching)

Design method applied: Jenike
Safety margin for Theta,c: 3.0°. Safety factor for ff: 1.00; extended PHIE range (20°..80°)

Results based on interpolation between test data: black
Results based on extrapolation: red

Minimum outlet diameter to avoid arching, corresponding maximum hopper wall slope to obtain mass flow, and critical values of flow properties:

Time [h]	SIGMA1,cr [Pa]	SIGMAW,cr [Pa]	FC,cr [Pa]	RHOB,cr [kg/m³]	PHIE,cr [°]	PHIX,cr [°]	PHILIN,cr [°]
0	1803	1223	1544	975	54.4	32.4	39.9
4.00	4564	3576	3666	1056	52.0	25.8	38.9
8.00	5634	4469	4471	1069	51.0	25.1	38.5

Time [h]	Theta,c [°]	ff [-]	H [-]	d,cr [m]	q [-]	SIGMAV,cr [Pa]
0	8.5	1.172	2.13	0.344	0.145	608
4.00	16.2	1.244	2.25	0.796	0.155	1626
8.00	17.0	1.259	2.26	0.964	0.158	2033

Time [h]	Comment
0	
4.00	
8.00	

Hopper wall slope in dependence on local hopper diameter

Here you can find the maximum hopper wall slope against the vertical as a function of the local hopper diameter.
Important: This is NO statement on the minimum outlet diameter to avoid arching!

d [m]	Theta,c [°]	d [m]	Theta,c [°]	d [m]	Theta,c [°]	d [m]	Theta,c [°]	d [m]	Theta,c [°]
0.2398	0.0	0.4397	11.8	1.1400	17.7	2.1398	19.1	-	-
0.2498	1.4	0.4798	12.6	1.2410	17.9	2.2405	19.2	-	-
0.2598	2.6	0.5213	13.4	1.3404	18.2	2.3402	19.2	-	-
0.2698	3.6	0.5603	14.0	1.4401	18.4	2.4401	19.3	-	-
0.2798	4.6	0.6014	14.5	1.5399	18.6	2.5399	19.3	-	-
0.2997	6.1	0.6401	14.9	1.6405	18.7	2.6406	19.4	-	-
0.3197	7.3	0.7399	15.8	1.7400	18.9	2.7398	19.4	-	-
0.3397	8.4	0.8405	16.4	1.8411	19.0	2.8405	19.4	-	-
0.3597	9.2	0.9402	16.9	1.9406	19.0	-	-	-	-
0.3997	10.7	1.0397	17.3	2.0410	19.1	-	-	-	-

Minimum outlet diameter to avoid arching in dependence on hopper wall slope and storage time at rest

Here you can find the minimum outlet diameter d to avoid arching for the measured storage times as a function of hopper wall slope Theta.
Green dimensions result from mass flow boundary.

		Storage time t [h]			Unit
Theta,c [°]	0	4.00	8.00		
19.0	1.848	1.848	1.848	m	
18.0	1.253	1.253	1.253	m	
17.0	0.954	0.954	0.964	m	
16.0	0.768	0.794	0.953	m	
15.0	0.646	0.786	0.944	m	
14.0	0.580	0.779	0.934	m	
13.0	0.497	0.772	0.927	m	
12.0	0.449	0.766	0.921	m	
11.0	0.410	0.760	0.914	m	
10.0	0.379	0.755	0.909	m	
9.0	0.354	0.751	0.903	m	
8.0	0.343	0.747	0.900	m	
7.0	0.340	0.743	0.896	m	
6.0	0.337	0.739	0.893	m	
5.0	0.334	0.737	0.891	m	
4.0	0.331	0.735	0.889	m	
3.0	0.329	0.733	0.888	m	
2.0	0.326	0.731	0.888	m	
1.0	0.324	0.731	0.889	m	

Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta, c [°]

3

ff (MF)

1

My Silo (data input)

Theta [°]

20

b, d [m]

0.5

Hopper shape

☒ Cone
☐ Wedge
☐ Asym. wedge

More settings

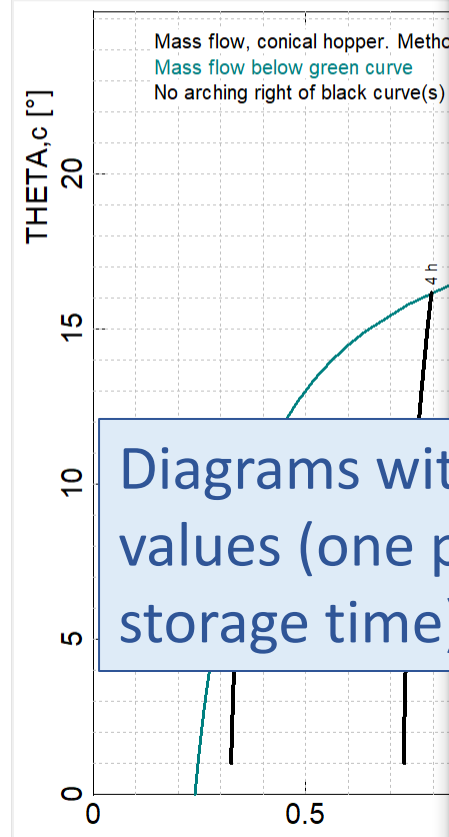
▶ CALCULATE

📄

CREATE PDF

Yield loci	Wall friction	Time
MF: Theta = f(b,d)		MF: d = f(b,d)
Theta, c [°] t [h]	0	4.00
19.0	1.848	1.848
18.0	1.253	1.253
17.0	0.954	0.954
16.0	0.768	0.794
15.0	0.646	0.786

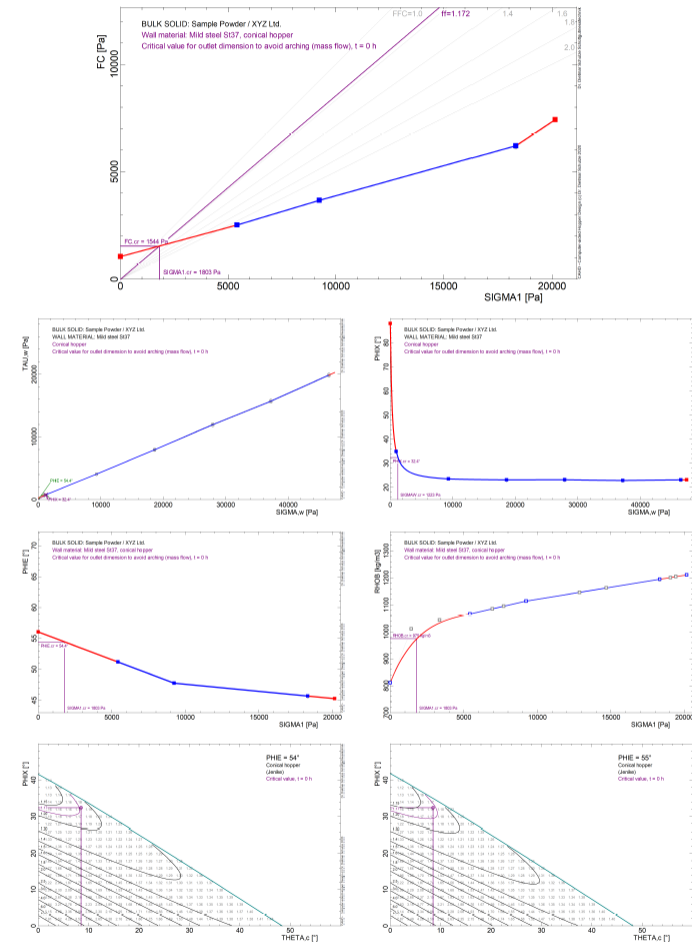
Flow function RHOB PHIE PHILIN P



Diagrams with critical values (one page per storage time)

CAHD v1.0.0.9 User: unknown 21.01.2021 16:26:46 page 4
Bulk solid: Sample Powder, Order: XYZ Ltd., Wall material: Mild steel St37

Hopper design diagrams: Conical hopper, Storage time 0 h, Mass flow



Yield loci

Time yield loci

Wall yield loci

Hopper Design

Edit flow properties

Edit cell

Reset:

Cell

Column

Table

All

Change WYL

WYL Reg

WYL SS

Safety for

Theta,c [°]

ff (MF)

3

1

My Silo (data input)

Theta [°]

b, d [m]

20

0.5

Hopper shape

☒ Cone

☐ Wedge

☐ Asym. wedge

More settings

CALCULATE

CREATE PDF

Yield loci

Wall friction

Time yield loci

MF: Theta = f(b,d)

MF: d = f(Theta)

Theta,c [°] t [h]	0	4.00
19.0	1.848	1.848
18.0	1.253	1.253
17.0	0.954	0.954
16.0	0.768	0.794
15.0	0.646	0.786

Flow function

RHOB

PHIE

PHILIN

P

Mass flow, conical hopper. Method: Jenike, Safety Theta: 3.0°, Ext. Range PHIE

Mass flow below green curve

No arching right of black curve(s)

Sample Powder_Mild steel St37.pdf - Adobe Acrobat Reader DC

Datei Bearbeiten Anzeige Unterschreiben Fenster Hilfe

Start Werkzeuge Sample Powder_Mil...

7 / 26 91%

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Bulk solid: Sample Powder, Order: XYZ Ltd., Wall material: Mild steel St37

Summary: Conical hopper, hopper wall slope and outlet diameter

Theta-d-diagram

More diagrams are included for wedge-shaped hoppers, asymmetric wedge-shaped hoppers, “My silo” , maximum outlet dimensions (in case of a second intersection of flow function with ff-line), arching and ratholing in case of funnel flow (upper bound, lower bound).

Zur Suche Text hier eingeben

**Thank you for your kind
attention.**